

Machine Learning: Introduction and Probability

Data Science School 2015
Dedan Kimathi University, Nyeri

Neil D. Lawrence

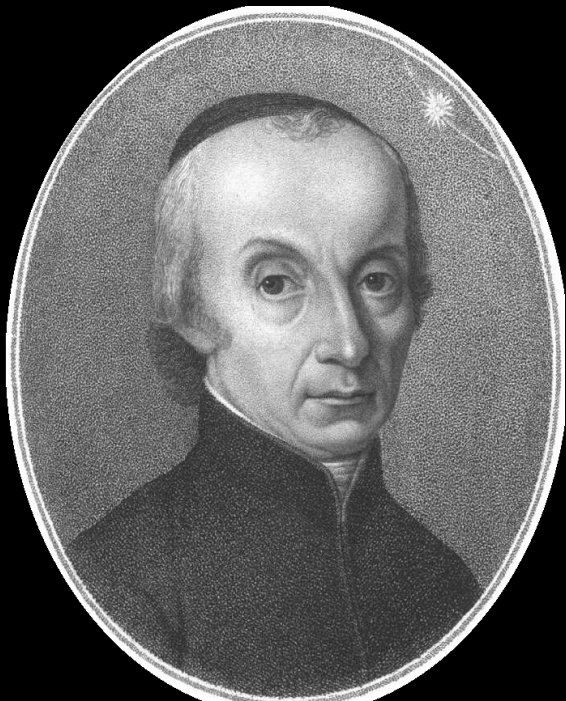
Department of Computer Science
Sheffield University

15th June 2015

Outline


Motivation

Machine Learning Books



Beobachtungen des zu Palermo d. 1. Jan. 1801 von Prof. Piazzi neu entdeckten Gasterms.

1801	Mittlere Sonnen-Zeit		Grade Aufst. in Zeit		Grade Auf- steigung in Gradon.		Nördl. Abweich.		Geocentri- sche Länge		Geocent. Breite		Ort der Sonne + 20" Abstraktion		Logar. d. Distanz ☉ ☿	
	St.	"	St.	"	"	"	"	"	Z.	"	Z.	"	Z.	"	"	"
Jan.	1	8 43 27,8	3 27 11,25	51 47 48,8	15 37 43,5	1 23 22 58,3	3 6 42,1	9 11 1 30,9	9,9926156							
	2	8 39 4,6	3 26 53,85	51 43 27,8	15 41 5,5	1 23 19 44,3	3 2 24,9	9 12 2 28,6	9,9926317							
	3	8 34 53,3	3 26 38,4	51 39 36,0	15 44 31,6	1 23 16 58,6	2 58 9,9	9 13 3 26,6	9,9926324							
	4	8 30 42,1	3 26 23,15	51 35 47,3	15 47 57,6	1 23 14 15,5	2 53 55,6	9 14 4 24,9	9,9926418							
	10	8 6 15,8	3 25 32,1	51 23 1,5	16 10 32,0	1 23 7 59,1	2 29 0,6	9 20 10 17,5	9,9927641							
	11	8 2 17,5	3 25 29,73	51 22 26,6												
	13	7 54 26,2	3 25 30,30	51 22 34,5	16 22 49,5	1 23 10 27,6	2 16 59,7	9 23 12 13,8	9,9928490							
	14	7 50 31,7	3 25 31,72	51 22 55,8	16 27 3,7	1 23 12 1,2	2 12 56,7	9 24 14 13,5	9,9928309							
	17				16 40 13,0											
	18	7 35 13,3	3 25 55,0	51 28 45,0												
	19	7 31 28,5	3 26 8,15	51 32 27,3	16 49 16,1	1 23 25 59,2	1 53 38,2	9 29 19 53,8	9,9930607							
	21	7 24 2,7	3 26 34,27	51 38 34,1	16 58 35,9	1 23 34 21,3	1 46 6,0	10 1 20 40,3	9,9931434							
	22	7 20 21,7	3 26 49,42	51 42 21,3	17 3 18,5	1 23 39 1,8	1 42 28,1	10 2 21 32,0	9,9931886							
	23	7 16 43,5	3 27 6,90	51 46 43,5	17 8 5,5	1 23 44 15,7	1 38 52,1	10 3 22 22,7	9,9932348							
	28	6 58 51,3	3 28 54,53	52 13 38,3	17 32 54,1	1 24 15 15,7	1 21 6,9	10 8 26 20,1	9,9935061							
	30	6 51 52,9	3 29 48,14	52 27 2,1	17 43 11,0	1 24 30 9,0	1 14 16,0	10 10 27 46,2	9,9936332							
	31	6 48 26,4	3 30 17,25	52 34 18,8	17 48 21,5	1 24 38 7,3	1 10 54,6	10 11 28 28,5	9,9937007							
Febr.	1	6 44 59,9	3 30 47,2	52 41 48,0	17 53 36,3	1 24 46 19,3	1 7 30,9	10 12 29 9,6	9,9937703							
	2	6 41 35,8	3 31 19,06	52 49 45,9	17 58 57,5	1 24 54 57,9	1 4 1,5	10 13 29 49,9	9,9938423							
	5	6 31 31,5	3 33 2,70	53 15 40,5	18 15 1,0	1 25 22 43,4	0 54 23,9	10 16 31 45,5	9,9940751							
	8	6 21 39,2	3 34 58,50	53 44 37,5	18 31 23,2	1 25 53 29,5	0 45 5,0	10 19 33 33,3	9,9943276							
	11	6 11 58,2	3 37 6,54	54 16 38,1	18 47 58,8	1 26 26 40,0	0 36 2,9	10 22 35 12,4	9,9945823							



1801/01/01
1801/01/04

× 1801/01/10

×× 1801/01/13

× 1801/01/19

××× 1801/01/22

× 1801/01/28

××× 1801/01/31

× 1801/02/05

× 1801/02/08

× 1801/02/11



hier in der Nähe der Quadratur der Einfluß der Sonne Länge geringer ist, als in andern Lagen. Dr. *Gauß* glaubt daher, daß es nicht unendlich wäre, wenn man die Fehler der Sonnentafeln aus sehr genauen Beobachtungen für diese Zeiten bestimmte, und die Örter der Sonne hiernach verbesserte. Diese vier Elemente sind nun folgende:

Sonnenferne	326° 07' 38"	Hieraus;
δ	81 0 44	größte Mittelp. Gief-
Neigung	10 36 57	chung 9° 27' 41"
Log. halb. gr. Axe	0,4420527	täg. mittlere helioc.
Excentricität	0,0825017	tropische Beweg. 770,914
Epoche 1800 31 Dec.	77° 36' 34"	

Aus diesen Elementen hat Dr. *Gauß* folgende Örter der *Ceres Ferdinānda* im voraus berechnet. Die Zeit ist mittlere für Mitternacht in *Palemo*.

1801	Geocen- trische Länge	Geo- centri- sche Breite nördl.	Logarith- des Ab- standes von der S	Logarith- des Ab- standes von der C	Verhält- nis der gelbe- nen Helligk.
	Z				
Nov. 25	5 20 16	9 25	0,42181	0,40468	0,6102
Dec. 1	5 22 15	9 48	0,40940	0,40472	0,6459
	7 5 24 7	10 12	0,39644	0,40479	0,6855
	13 5 25 51	10 37	0,38296	0,40488	0,7290
	19 5 27 27	11 4	0,36902	0,40499	0,7770
	25 5 28 53	11 32	0,35468	0,40512	0,8295
	31 6 0 10 12	11 0	0,34000	0,40528	0,8869

Sollte man den Ort des Planeten nach diesen Elementen genauer, oder auf eine längere Zeit berechnen wollen: so setzen wir zu diesem Behufe noch folgende Formeln hierher:

1) Zur

Epocha 1800 31 Dec. $77^{\circ} 36' 34''$

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 Örter der *Ceres Ferdinanda* im voraus berechnet.
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	Z				
Nov. 25	5 20 16	9 25	0, 42181	0, 40468	0, 6102
Dec. 1	5 22 15	9 48	0, 40940	0, 40472	0, 6459
	7 5 24 7	10 12	0, 39643	0, 40479	0, 6855
	13 5 25 51	10 37	0, 38296	0, 40488	0, 7290
	19 5 27 27	11 4	0, 36902	0, 40499	0, 7770
	25 5 28 53	11 32	0, 35468	0, 40512	0, 8295
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DELLA SCOPERTA
DEL NUOVO PIANETA
CERERE FERDINANDEA

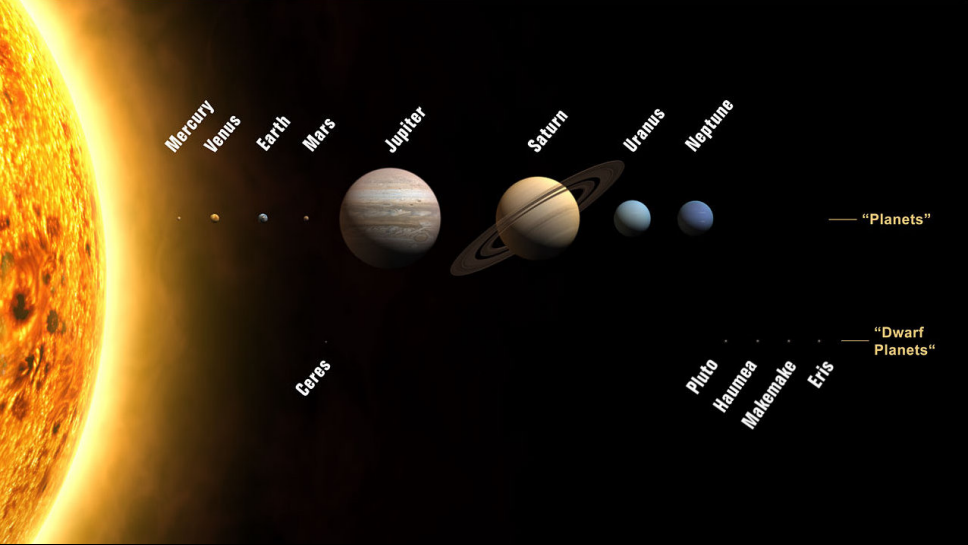
OTTAVO TRA I PRINCIPALJ DEL NOSTRO SISTEMA
SOLARE.



PALERMO
1802

NELLA STAMPERIA REALE.





Mercury

Venus

Earth

Mars

Jupiter

Saturn

Uranus

Neptune

— "Planets"

Ceres

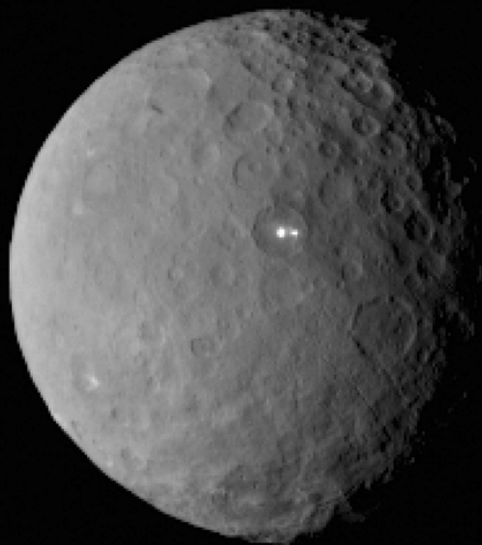
Pluto

Haumea

Makemake

Eris

— "Dwarf Planets"



What is Machine Learning?

data

- **data**: observations, could be actively or passively acquired (meta-data).
- **model**: assumptions, based on previous experience (other data! transfer learning etc), or beliefs about the regularities of the universe. Inductive bias.
- **prediction**: an action to be taken or a categorization or a quality score.

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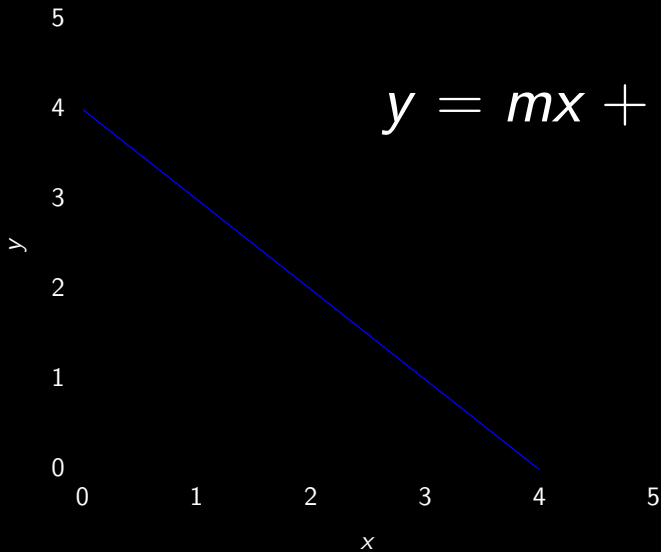
What is Machine Learning?

$$\text{data} + \text{model} = \text{prediction}$$

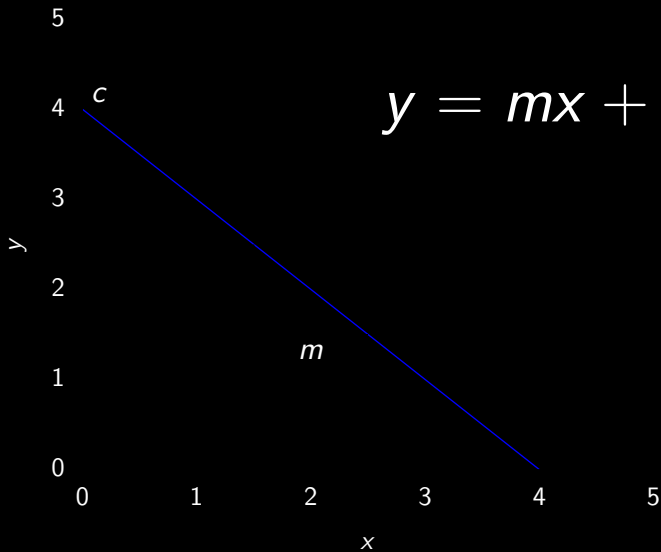
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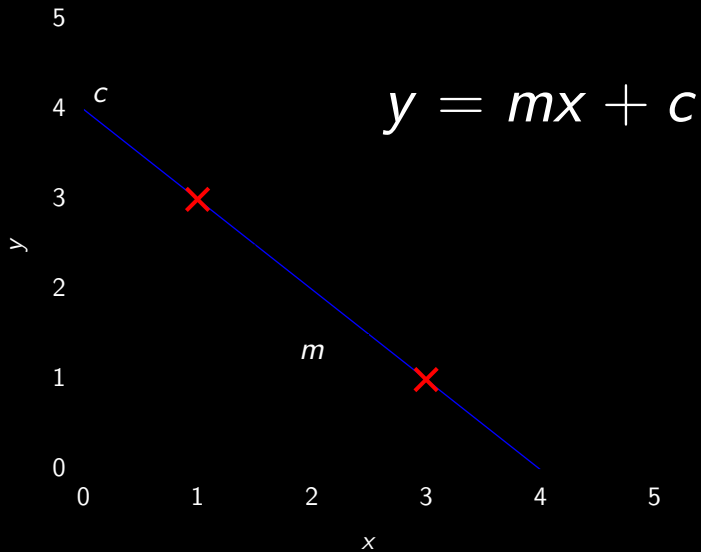
$$y = mx + c$$

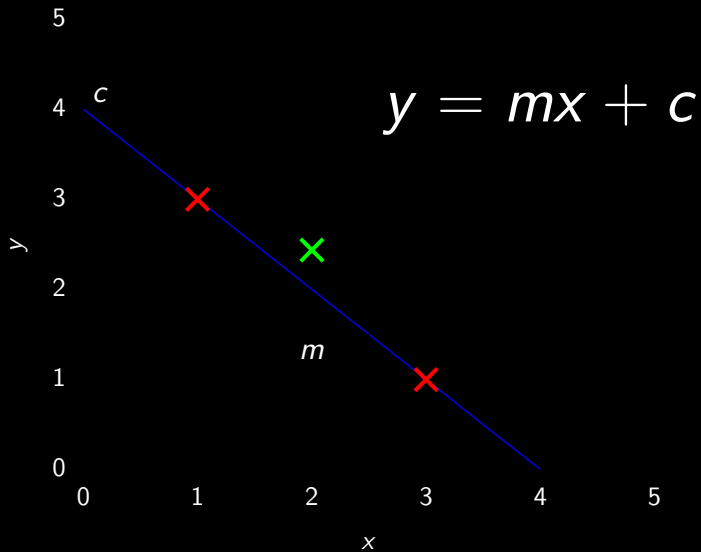
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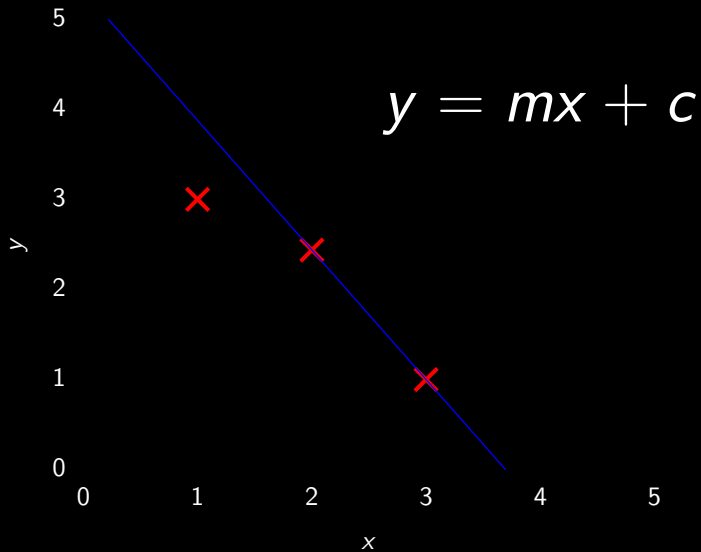


$$y = mx + c$$

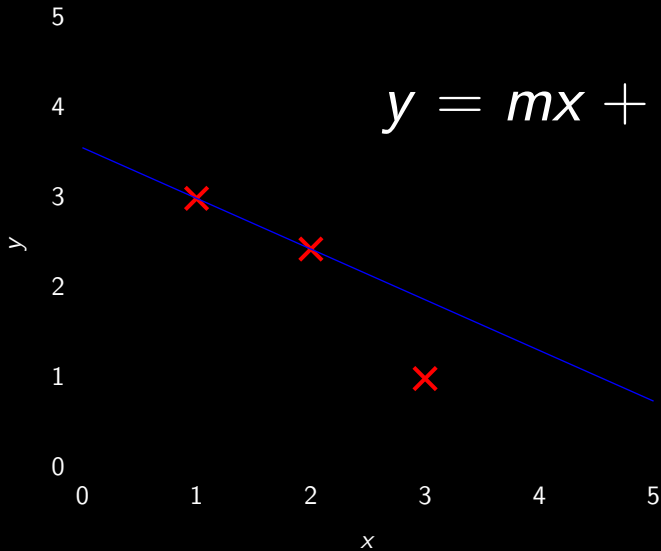


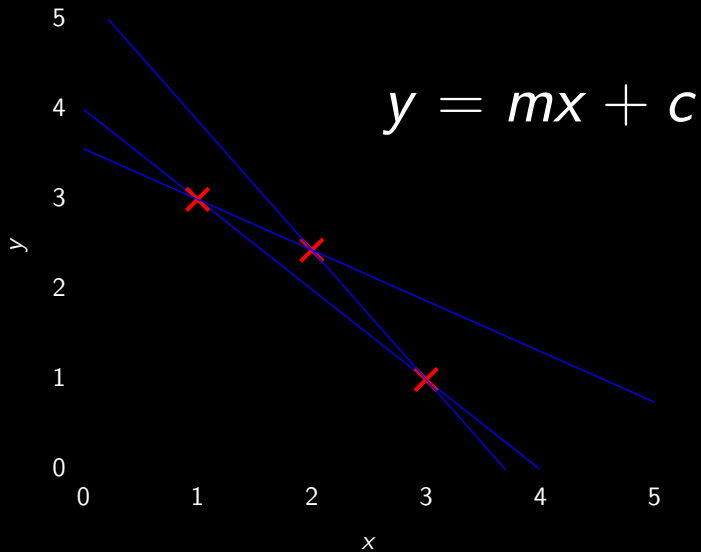






$$y = mx + c$$





$$y = mx + c$$

point 1: $x = 1, y = 3$

$$3 = m + c$$

point 2: $x = 3, y = 1$

$$1 = 3m + c$$

point 3: $x = 2, y = 2.5$

$$2.5 = 2m + c$$



riens. L'opinion contraire est une illusion de l'esprit qui, perdant de vue les raisons fugitives du choix de la volonté dans les choses indifférentes, se persuade qu'elle s'est déterminée d'elle-même et sans motifs.

Nous devons donc envisager l'état présent de l'univers, comme l'effet de son état antérieur, et comme la cause de celui qui va suivre. Une intelligence qui, pour un instant donné, connaîtrait toutes les forces dont la nature est animée, et la situation respective des êtres qui la composent, si d'ailleurs elle était assez vaste pour soumettre ces données à l'analyse, embrasserait dans la même formule les mouvemens des plus grands corps de l'univers et ceux du plus léger atome : rien ne serait incertain pour elle, et l'avenir comme le passé, serait présent à ses yeux. L'esprit humain offre, dans la perfection qu'il a su donner à l'Astronomie, une faible esquisse de cette intelligence. Ses découvertes en Mécanique et en Géométrie, jointes à celle de la pesanteur universelle, l'ont mis à portée de comprendre dans les mêmes expressions analytiques, les états passés et futurs du système du monde. En appliquant la même méthode à quelques autres objets de ses connaissances, il est parvenu à ramener à des lois générales, les phénomènes observés, et à prévoir ceux que des circonstances données doivent faire éclore. Tous ces efforts dans la recherche de la vérité, tendent à le rapprocher sans cesse de l'intelligence que nous venons de concevoir, mais dont il restera toujours infiniment éloigné. Cette tendance propre à l'espèce humaine, est ce qui la rend supérieure aux animaux; et ses progrès en ce genre, distinguent les nations et les siècles, et font leur véritable gloire.

Rappelons-nous qu'autrefois, et à une époque qui

other, we say that its choice is an effect without a cause. It is then, says Leibnitz, the blind chance of the Epicureans. The contrary opinion is an illusion of the mind, which, losing sight of the evasive reasons of the choice of the will in indifferent things, believes that choice is determined of itself and without motives.

We ought then to regard the present state of the universe as the effect of its anterior state and as the cause of the one which is to follow. Given for one instant an intelligence which could comprehend all the forces by which nature is animated and the respective situation of the beings who compose it—an intelligence sufficiently vast to submit these data to analysis—it would embrace in the same formula the movements of the greatest bodies of the universe and those of the lightest atom; for it, nothing would be uncertain and the future, as the past, would be present to its eyes. The human mind offers, in the perfection which it has been able to give to astronomy, a feeble idea of this intelligence. Its discoveries in mechanics and geometry, added to that of universal gravity, have enabled it to comprehend in the same analytical expressions the past and future states of the system of the world. Applying the same method to some other objects of its knowledge, it has succeeded in referring to general laws observed phenomena and in foreseeing those which given circumstances ought to produce. All these efforts in the search for truth tend to lead it back continually to the vast intelligence which we have just mentioned, but from which it will always remain infinitely removed. This tendency, peculiar to the human race, is that which renders it superior to animals; and their progress

height: "The day will come when, by study pursued through several ages, the things now concealed will appear with evidence; and posterity will be astonished that truths so clear had escaped us." Clairaut then undertook to submit to analysis the perturbations which the comet had experienced by the action of the two great planets, Jupiter and Saturn; after immense calculations he fixed its next passage at the perihelion toward the beginning of April, 1759, which was actually verified by observation. The regularity which astronomy shows us in the movements of the comets doubtless exists also in all phenomena. -

The curve described by a simple molecule of air or vapor is regulated in a manner just as certain as the planetary orbits; the only difference between them is that which comes from our ignorance.

Probability is relative, in part to this ignorance, in part to our knowledge. We know that of three or a greater number of events a single one ought to occur; but nothing induces us to believe that one of them will occur rather than the others. In this state of indecision it is impossible for us to announce their occurrence with certainty. It is, however, probable that one of these events, chosen at will, will not occur because we see several cases equally possible which exclude its occurrence, while only a single one favors it.

The theory of chance consists in reducing all the events of the same kind to a certain number of cases equally possible, that is to say, to such as we may be equally undecided about in regard to their existence, and in determining the number of cases favorable to the event whose probability is sought. The ratio of

$$y = mx + c + \epsilon$$

point 1: $x = 1, y = 3$

$$3 = m + c + \epsilon_1$$

point 2: $x = 3, y = 1$

$$1 = 3m + c + \epsilon_2$$

point 3: $x = 2, y = 2.5$

$$2.5 = 2m + c + \epsilon_3$$

Applications of Machine Learning

Handwriting Recognition : Recognising handwritten characters.

For example LeNet <http://bit.ly/d26fwK>.

Friend Identification : Suggesting friends on social networks

[https://](https://www.facebook.com/help/501283333222485)

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Ranking : Learning relative skills of on line game players, the

TrueSkill system <http://research.microsoft.com/en-us/projects/trueskill/>.

Collaborative Filtering : Prediction of user preferences for items given purchase history. For example the Netflix Prize

<http://www.netflixprize.com/>.

Internet Search : For example Ad Click Through rate prediction

<http://bit.ly/a7XLH4>.

News Personalisation : For example Zite <http://www.zite.com/>.

Game Play Learning : For example, learning to play Go

<http://bit.ly/cV77zM>.

History of Machine Learning (personal)

Rosenblatt to Vapnik

- Arises from the Connectionist movement in AI.
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Frank Rosenblatt's Perceptron

- Rosenblatt's perceptron (Rosenblatt, 1962) based on simple model of a neuron (McCulloch and Pitts, 1943) and a learning algorithm.



Figure : Frank Rosenblatt in 1950 (source: Cornell University Library)

Vladimir Vapnik's Statistical Learning Theory

- Later machine learning research focused on theoretical foundations of such models and their capacity to learn (Vapnik, 1998).

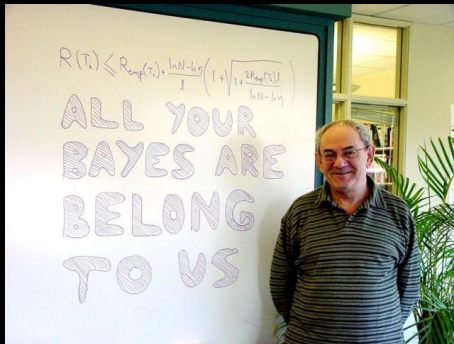


Figure : Vladimir Vapnik "All Your Bayes ..." (source <http://lecun.com/ex/fun/index.html>), see also <http://bit.ly/qfd2mU>.

Personal View

- Machine learning benefited greatly by incorporating ideas from psychology, but not being afraid to incorporate rigorous theory.

Machine Learning Today

An extension of statistics?

- Early machine learning viewed with scepticism by statisticians.
- Modern machine learning and statistics interact to both communities benefits.
- *Personal view:* statistics and machine learning are fundamentally different. Statistics aims to provide a human with the tools to analyze data. Machine learning wants to replace the human in the processing of data.

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Machine Learning Today

Mathematics and Bumblebees

- For the moment the two overlap strongly. But they are not the same field!
- Machine learning also has overlap with Cognitive Science.
- Mathematical formalisms of a problem are helpful, but they can hide facts: i.e. the fallacy that “aerodynamically a bumble bee can’t fly”. Clearly a limitation of the model rather than fact.
- Mathematical foundations are still very important though: they help us understand the capabilities of our algorithms.
- But we mustn't restrict our ambitions to the limitations of current mathematical formalisms. That is where humans give inspiration.

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Statistics

What's in a Name?

- Early statistics had great success with the idea of statistical proof.

Question: I computed the mean of these two tables of numbers (a statistic). They are different. Does this "prove" anything?

Answer: it depends on how the numbers are generated, how many there are and how big the difference. Randomization is important.

- Hypothesis testing: questions you can ask about your data are quite limiting.
- This can have the affect of limiting science too.
- Many successes: crop fertilization, clinical trials, brewing, polling.
- Many open questions: e.g. causality.

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Early 20th Century Statistics

- Many statisticians were Edwardian English gentleman.



Figure : William Sealy Gosset in 1908

Statistics and Machine Learning

*Statisticians want to turn humans into computers.
Machine learners want to turn computers into humans.
We meet somewhere in the middle.*

NDL 2012/06/16

Statistics

- Cricket and Baseball are two games with a lot of “statistics”.
- The study of the meaning behind these numbers is “mathematical statistics” often abbreviated to “statistics”.

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Aleatoric uncertainty: uncertainty arising through an underlying stochastic system. (Where will a sheet of paper fall if I drop it?)

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Aleatoric uncertainty: uncertainty arising through an underlying stochastic system. (Where will a sheet of paper fall if I drop it?)

Probability: A Framework to Characterise Uncertainty

- We need a framework to characterise the uncertainty.
- In this course we make use of probability theory to characterise uncertainty.

Probability: A Framework to Characterise Uncertainty

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Richard Price

- Welsh philosopher and essay writer.
- Edited **Thomas Bayes**'s essay which contained foundations of Bayesian philosophy.

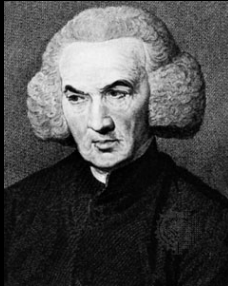


Figure : Richard Price, 1723–1791. (source Wikipedia)

Laplace

- French Mathematician and Astronomer.



Figure : Pierre-Simon Laplace, 1749–1827. (source Wikipedia)

Outline

Motivation

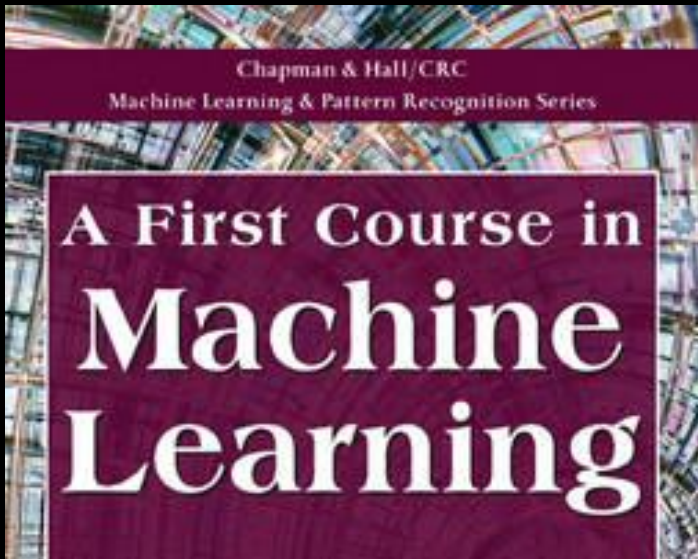
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