

# Bridging the Gap Between Computational Biology and Systems Biology

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University of Sheffield  
PathSoc Summer Meeting

4th July 2012

# Outline

Motivation

Cascade Differential Equations

Discussion and Future Work

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# Can a Biologist Fix a Radio? Lazebnik (2002)

## The Case for Systems Biology

*"It is difficult to find a black cat in a dark room,  
especially if there is no cat."*

- ▶ Biological systems are immensely complicated.
- ▶ Lazebnik argues the need for models that are quantitative.
  - ▶ Such models should be predictive of biological behaviour.
  - ▶ Such models need to be combined with biological data.
- ▶ Systems biology:
  - ▶ Build mechanistic models (based on biochemical knowledge) of the system.
  - ▶ Identify modules, submodules, and parameterize the models.

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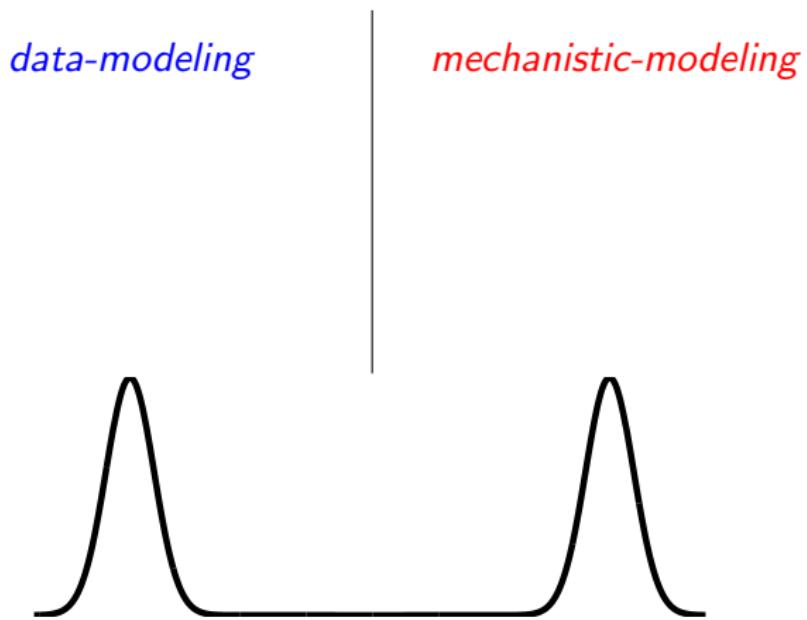
# Coregulation of Gene Expression

## The Case for Computational Biology

- ▶ Gene Expression to Transcriptional Regulation.
- ▶ A “data exploration” problem (computational biology/bioinformatics):
  - ▶ Use gene expression data to speculate on coregulated genes.
  - ▶ Traditionally use clustering of gene expression profiles.
- ▶ Contrast with (computational) systems biology approach:
  - ▶ Detailed mechanistic model of the system is created.
  - ▶ Fit parameters of the model to data.
  - ▶ Problematic for large data (genome wide).
  - ▶ Need to deal with unobserved biochemical species (TFs).

# Computational Biology vs Computational Systems Biology

Broadly Speaking: Two approaches to modeling



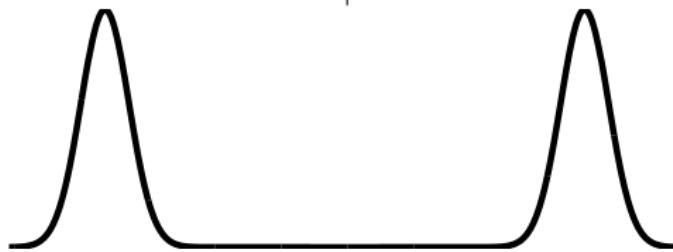
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let the data “speak”

*mechanistic-modeling*



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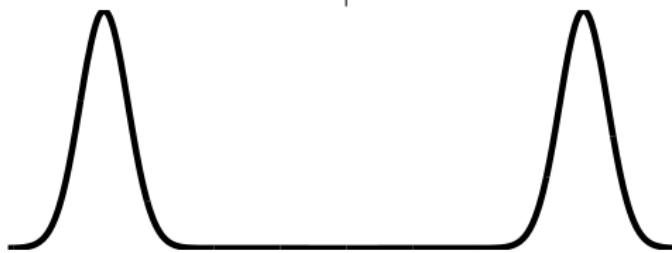
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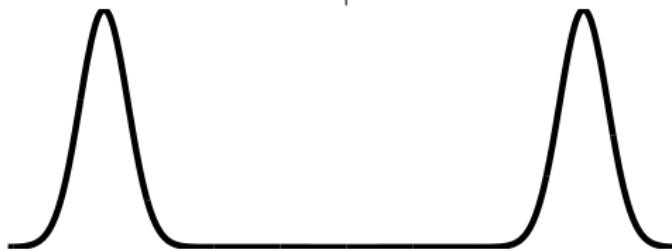
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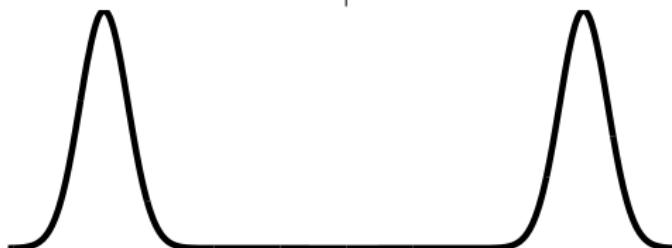
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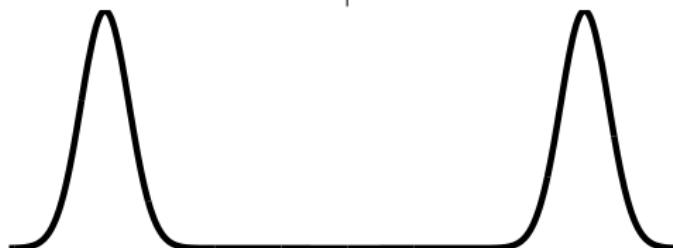
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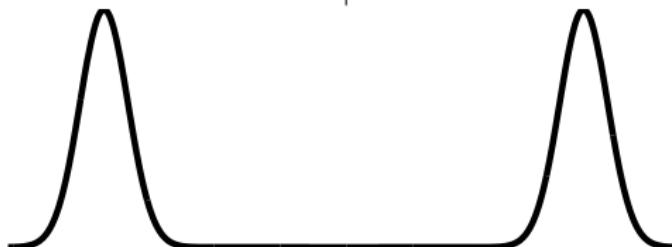
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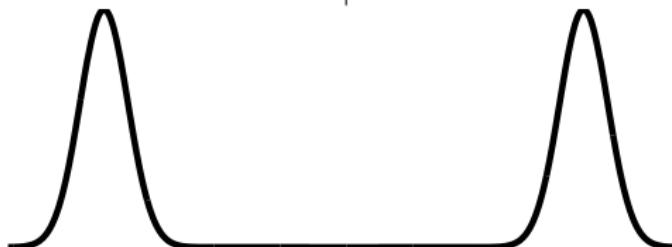
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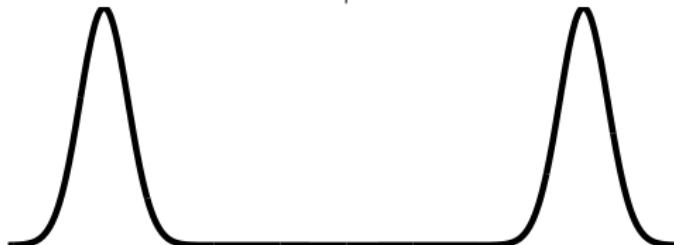
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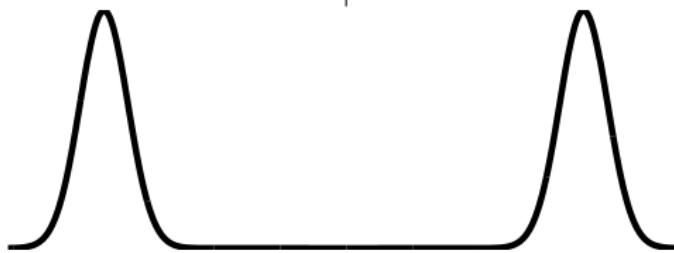
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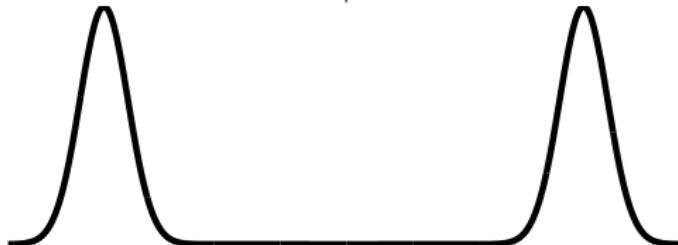
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differential equations  
SDE, ODE models

*Strongly Mechanistic*



# A Hybrid Approach

Introduce aspects of systems biology to computational models

- ▶ We advocate an approach *between* systems and computational biology.
- ▶ Introduce aspects of systems biology to the computational approach.
  - ▶ There is a computational penalty, but it may be worth paying.
  - ▶ Ideally there should be a smooth transition from pure computational (PCA, clustering, SVM classification) to systems (non-linear (stochastic) differential equations).
  - ▶ This work is one part of that transition.

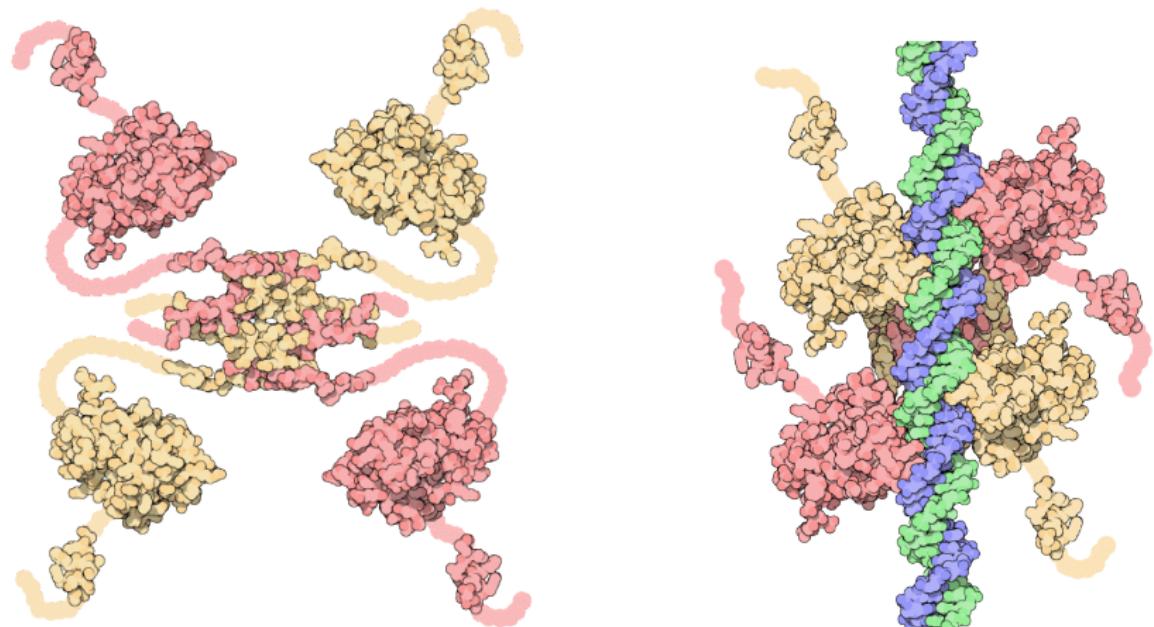
# Radiation Damage in the Cell

- ▶ Radiation can damage molecules including DNA.
- ▶ Most DNA damage is quickly repaired—single strand breaks, backbone break.
- ▶ Double strand breaks are more serious—a complete disconnect along the chromosome.
- ▶ Cell cycle stages:
  - ▶  $G_1$ : Cell is not dividing.
  - ▶  $G_2$ : Cell is preparing for mitosis, chromosomes have divided.
  - ▶ S: Cell is undergoing mitosis (DNA synthesis).
- ▶ Main problem is in  $G_1$ . In  $G_2$  there are two copies of the chromosome. In  $G_1$  only one copy.

## p53 “Guardian of the Cell”

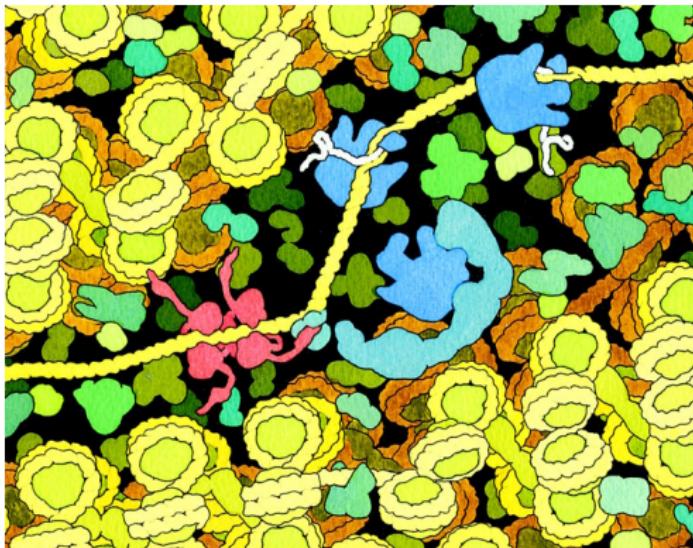
- ▶ Responsible for Repairing DNA damage
- ▶ Activates DNA Repair proteins
- ▶ Pauses the Cell Cycle (prevents replication of damage DNA)
- ▶ Initiates *apoptosis* (cell death) in the case where damage can't be repaired.
- ▶ Large scale feedback loop with NF- $\kappa$ B.

# p53 DNA Damage Repair



**Figure:** p53. *Left* unbound, *Right* bound to DNA. Images by David S. Goodsell from <http://www.rcsb.org/> (see the "Molecule of the Month" feature).

p53



**Figure:** Repair of DNA damage by p53. Image from Goodsell (1999).

## Some p53 Targets

*DDB2* DNA Damage Specific DNA Binding Protein 2. (also governed by C/ EBP-beta, E2F1, E2F3,...).

*p21* Cyclin-dependent kinase inhibitor 1A (CDKN1A). A regulator of cell cycle progression. (also governed by SREBP-1a, Sp1, Sp3,... ).

*hPA26/SESN1* sestrin 1 Cell Cycle arrest.

*BIK* BCL2-interacting killer. Induces cell death (apoptosis)

*TNFRSF10b* tumor necrosis factor receptor superfamily, member 10b. A transducer of apoptosis signals.

# Modelling Assumption

- ▶ Assume p53 affects targets as a single input module network motif (SIM).

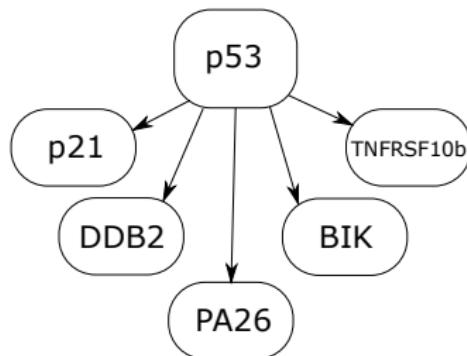


Figure: p53 SIM network motif as modelled by Barenco et al. 2006.

# Standard Approach

## Clustering of Gene Expression Profiles

- ▶ Assume that coregulated genes will cluster in the same groups.
- ▶ Perform clustering, and look for clusters containing target genes.
- ▶ These are candidates, look for confirmation in the literature etc.

# Mathematical Model

Method

Open Access

## Ranked prediction of p53 targets using hidden variable dynamic modeling

Martino Barenco<sup>\*†</sup>, Daniela Tomescu<sup>\*</sup>, Daniel Brewer<sup>\*†</sup>, Robin Callard<sup>\*†</sup>, Jaroslav Stark<sup>†‡</sup> and Michael Hubank<sup>\*†</sup>

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Correspondence: Michael Hubank. Email: m.hubank@ich.ucl.ac.uk

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Accepted: 21 February 2006

# Transcription Model

mRNA  
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rate

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$$\frac{\text{mRNA}}{\text{production rate}} = \frac{\text{base}}{\text{rate}}$$

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## Transcription Model

$$\text{mRNA production rate} = \text{base rate} + \text{TF activity} - \text{mRNA decay}$$

## Mathematical Model

- ▶ Differential equation model of system.

rate of mRNA transcription, baseline transcription rate,  
transcription factor activity, mRNA decay

- ▶ We have observations of  $m_j(t)$  from gene expression.

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$$\frac{dm_j(t)}{dt} = b_j + s_j p(t) - d_j m_j(t)$$

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- ▶ Fit parameters by maximum likelihood or MCMC sampling.

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- ▶ Clustering model is equivalent to assuming  $d_j$ ,  $b_j$ , and  $s_j$  are v. large.

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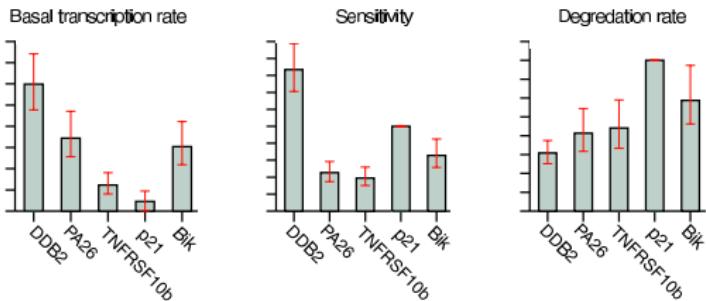
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- ▶ We have observations of  $m_j(t)$  from gene expression.
- ▶ Reorder differential equation and ignore gradient term.
- ▶ This suggests genes are scaled and offset versions of the TF.
- ▶ By normalizing data and clustering we hope to find those TFs.

# Response of p53

(a)



(b)

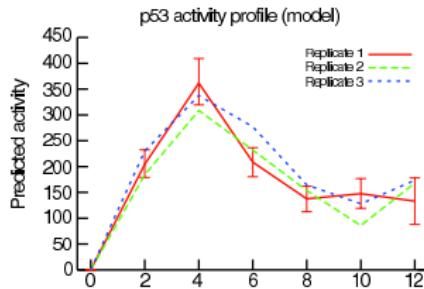
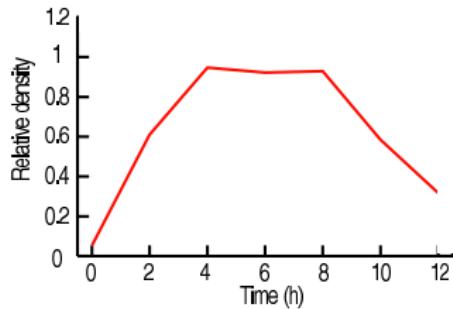
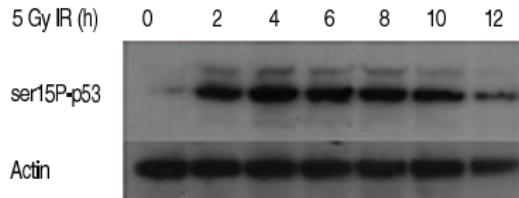


Figure: Results from Barenco et al. (2006). Top is parameter estimates. Bottom is inferred profile.

## Response to p53 ...



**Figure:** Results from Barenco et al. (2006). Activity profile of p53 was measured by Western blot to determine the levels of ser-15 phosphorylated p53 (ser15P-p53).

# Bayesian Inference for Functions

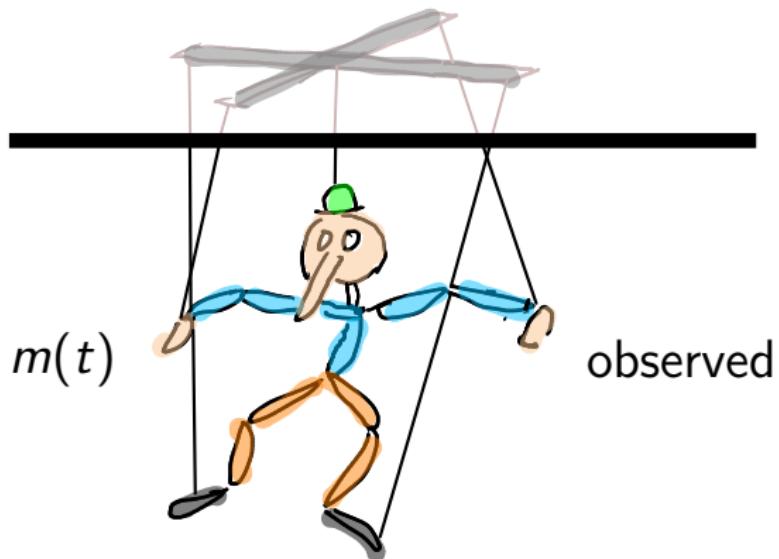
- ▶ Bayesian inference is a framework for dealing with *uncertainty*.
- ▶ From a modeling perspective, value of active TF over time,  $p(t)$ , is a *latent* variable.
- ▶ Latent variables are endemic, for example “Spot the Ball”.

# Spot the Ball

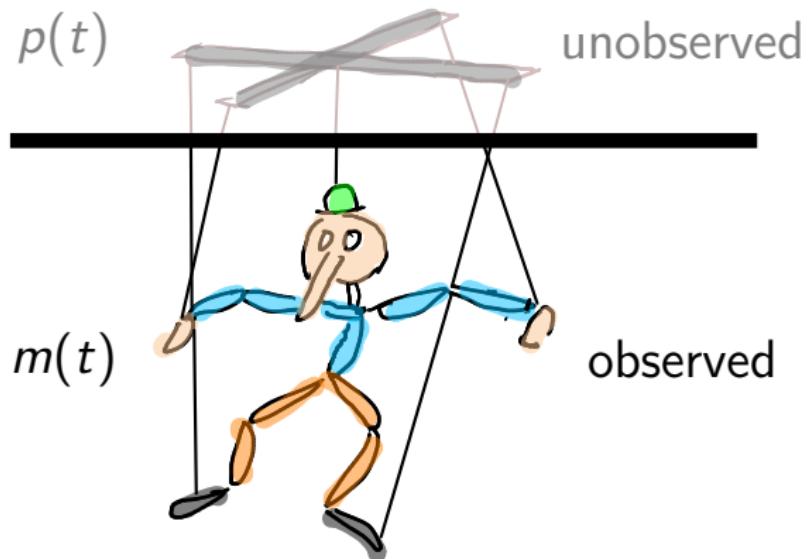


Image from <http://www.bluesmuse.com>

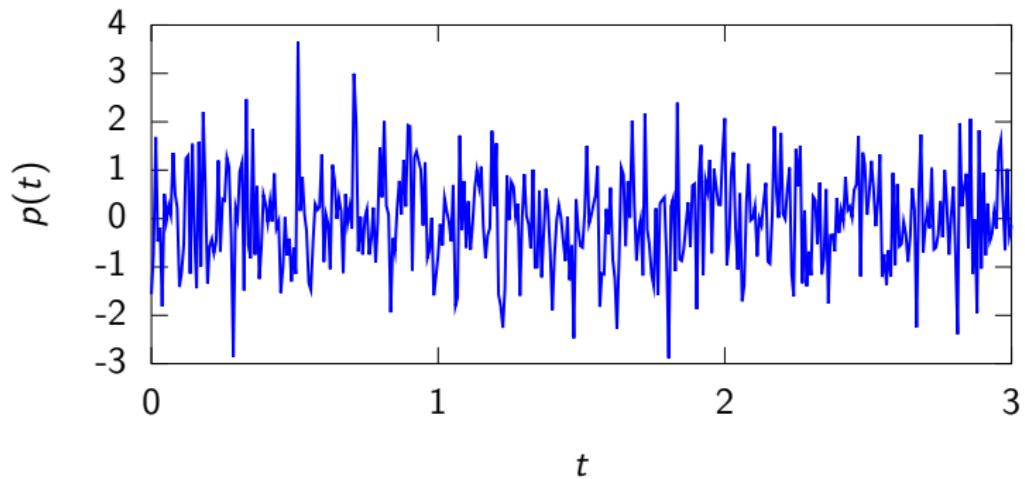
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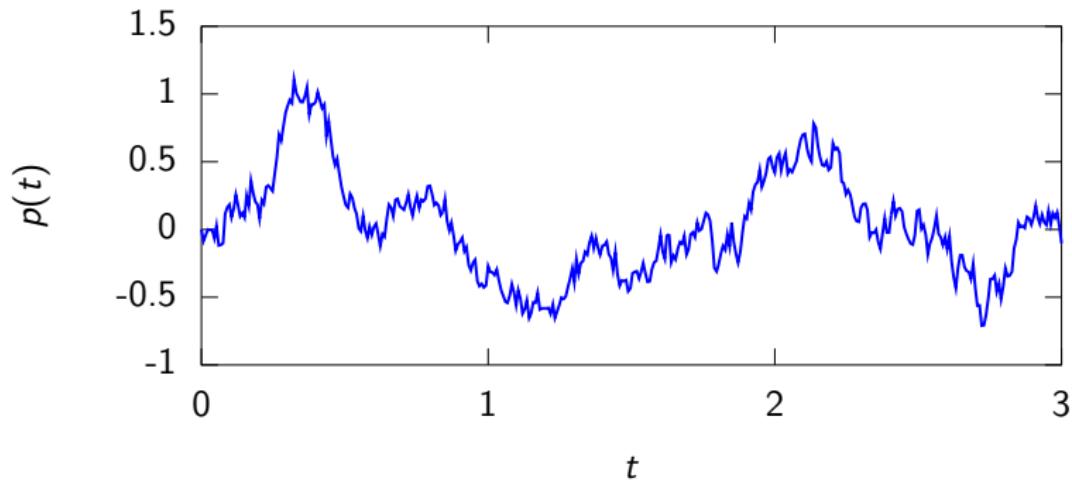


## Dimensionality Reduction: Temporal Data



**Figure:** PCA: Pure sampling from a Gaussian does not retain temporal effects.

## Dimensionality Reduction: Temporal Data



**Figure:** Kalman filter (Rauch-Tung-Striebel smoother) is Markov-Gaussian (non smooth).

## Dimensionality Reduction: Temporal Data

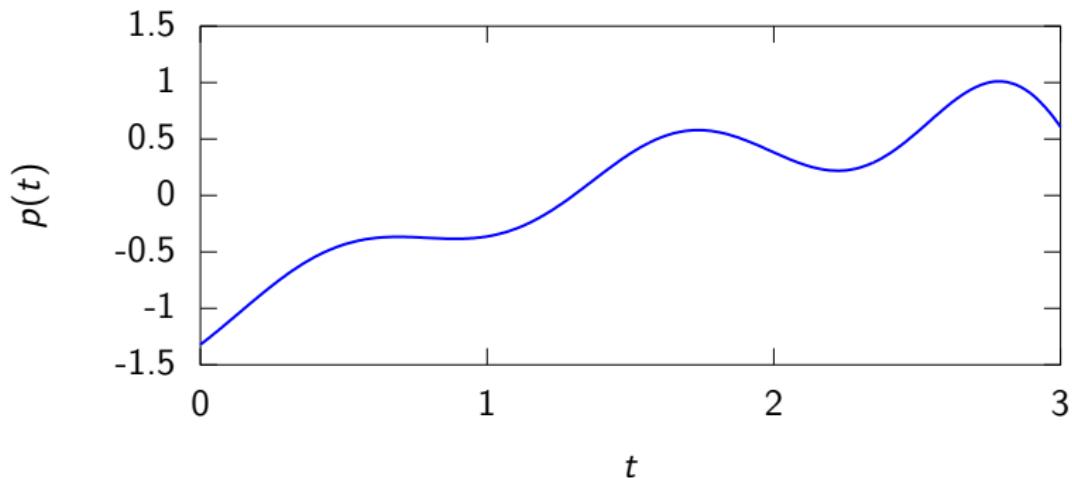
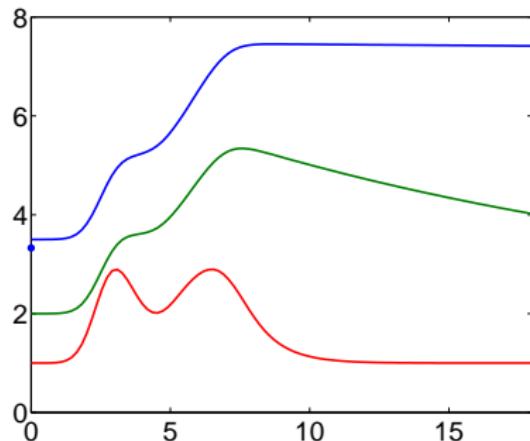


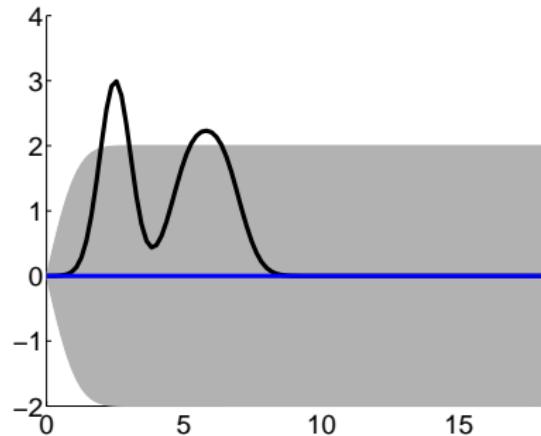
Figure: General Gaussian processes allow for priors over *smooth* functions.

# Artificial Example: Inferring $p(t)$

Inferring TF activity from artificially sampled genes.



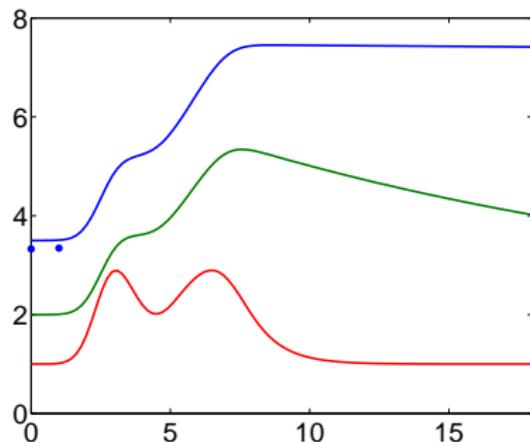
True “gene profiles” and noisy observations.



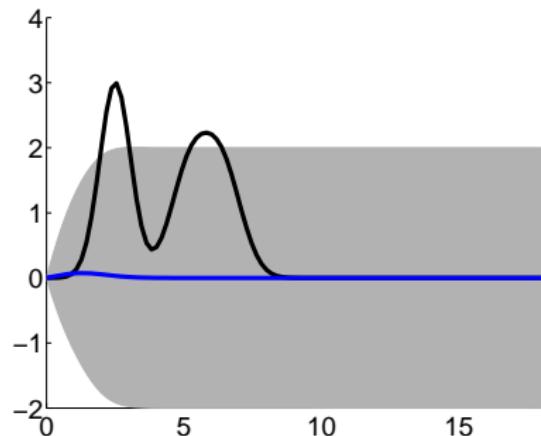
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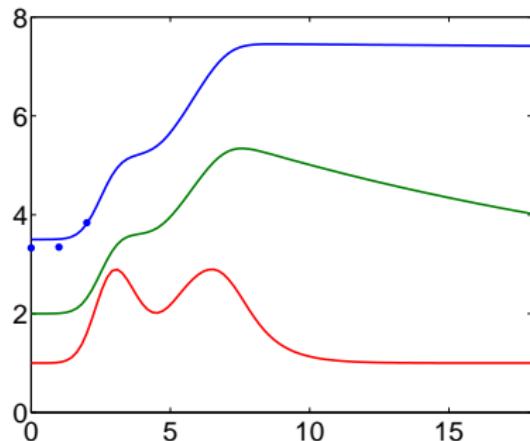
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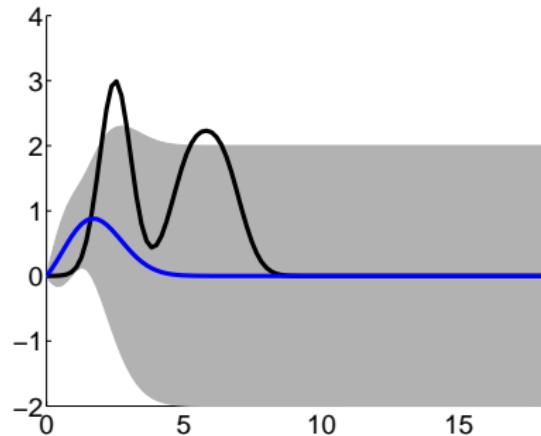
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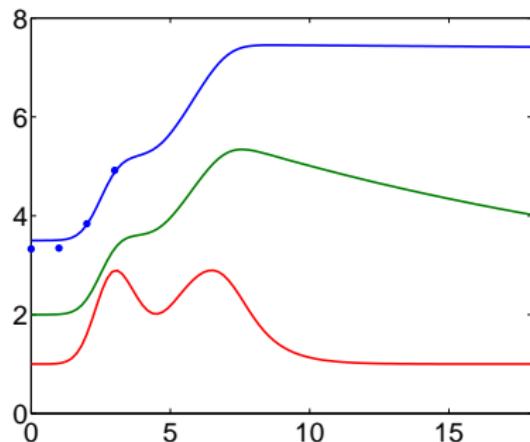
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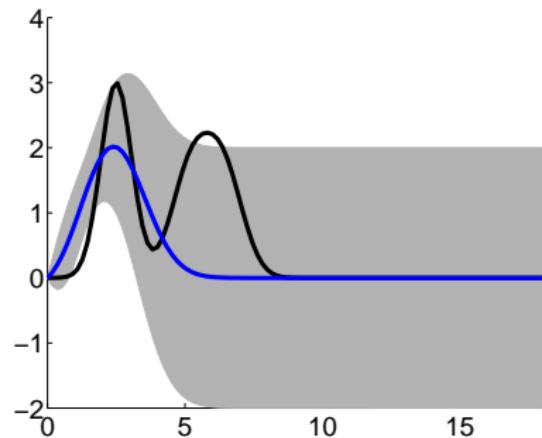
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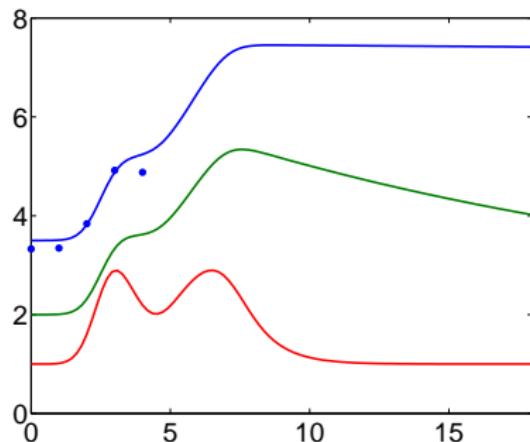
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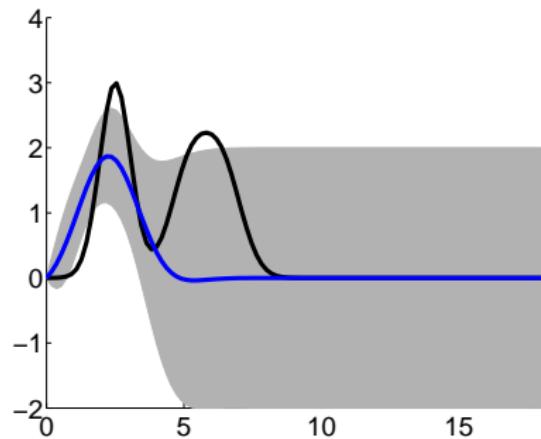
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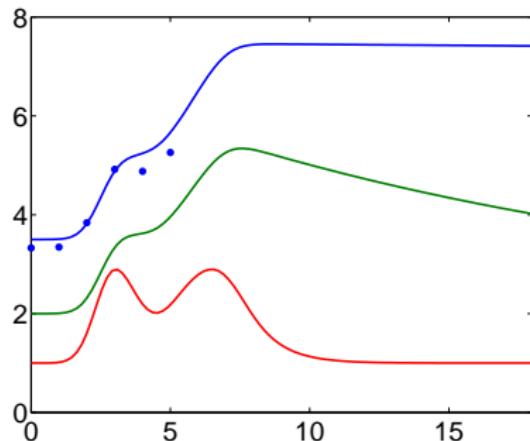
True “gene profiles” and noisy observations.



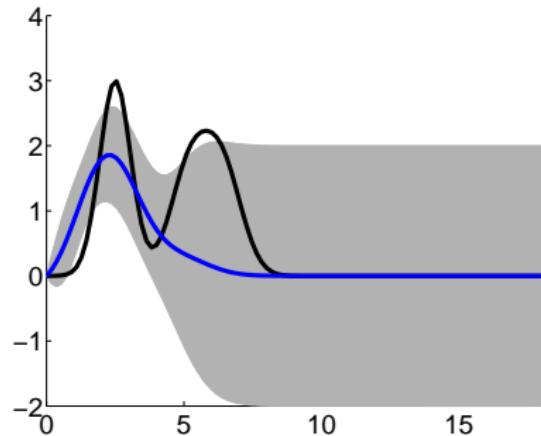
Inferred transcription factor activity.

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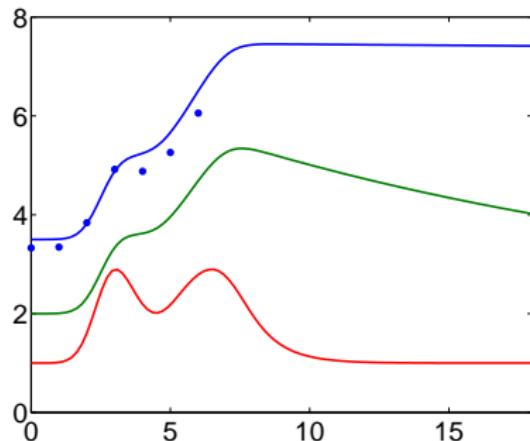
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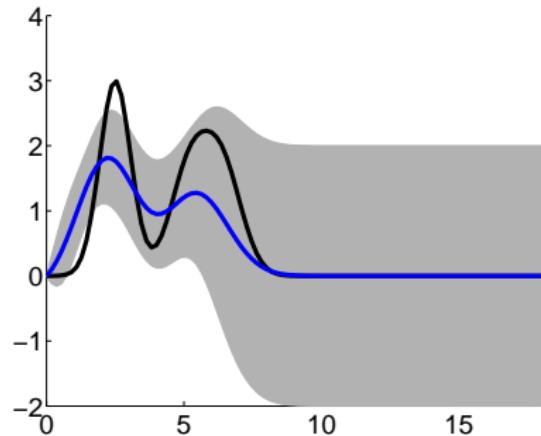
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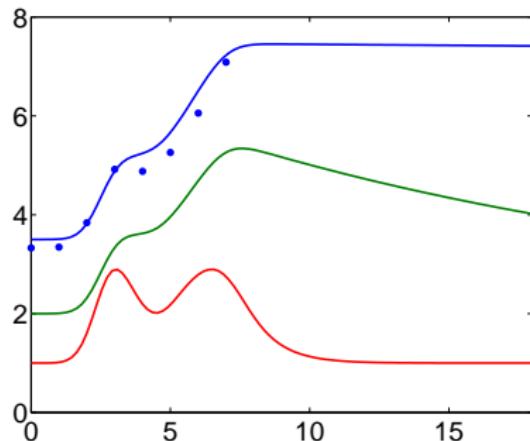
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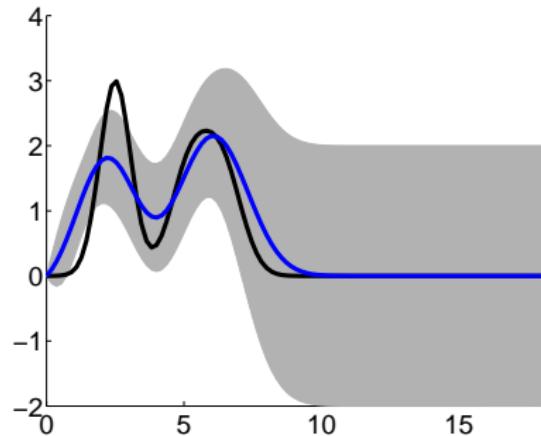
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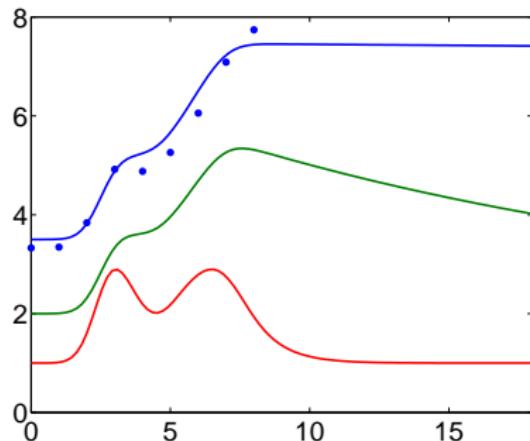
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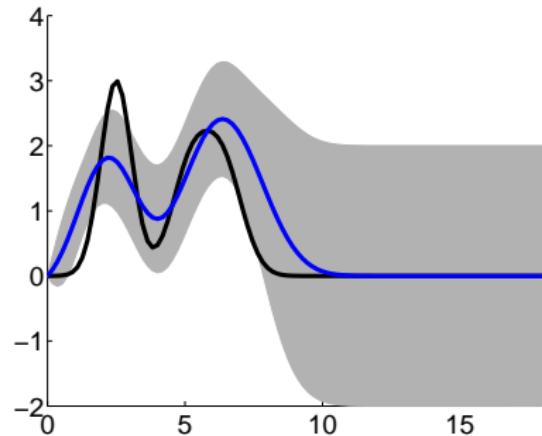
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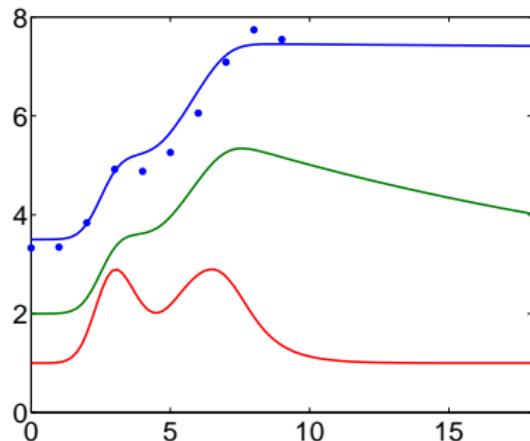
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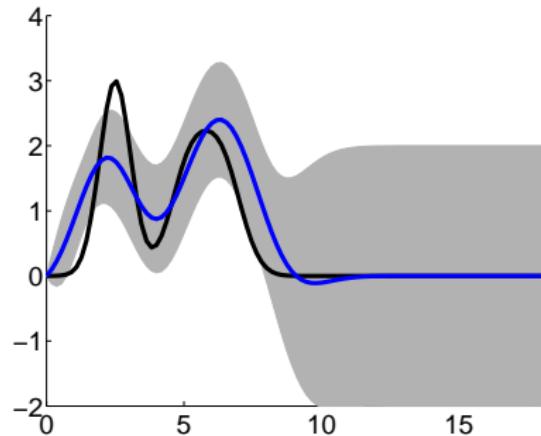
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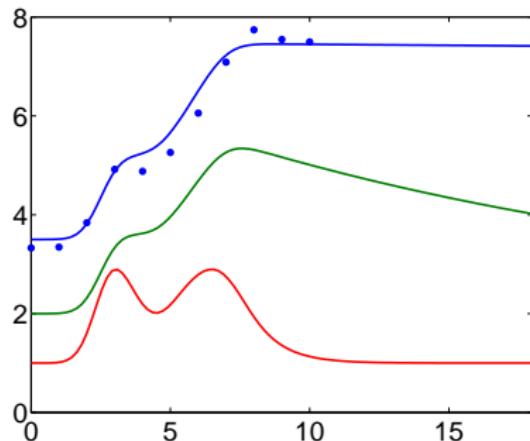
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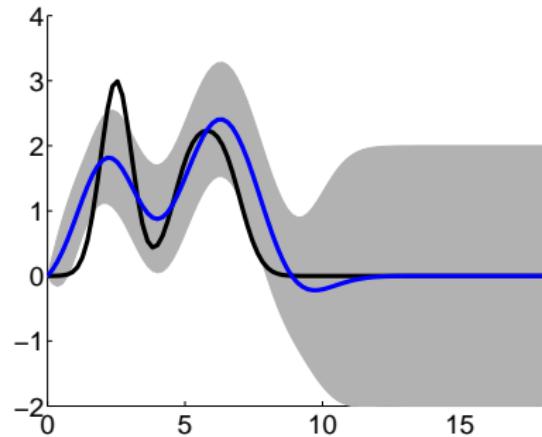
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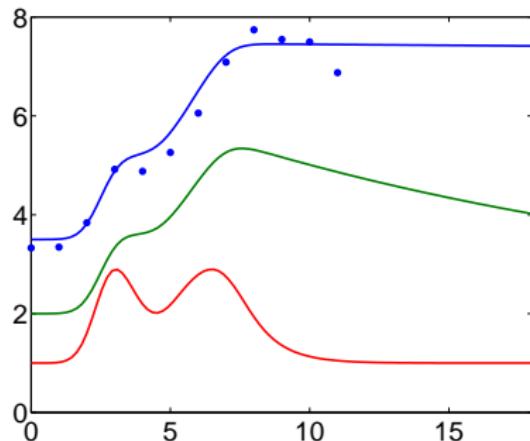
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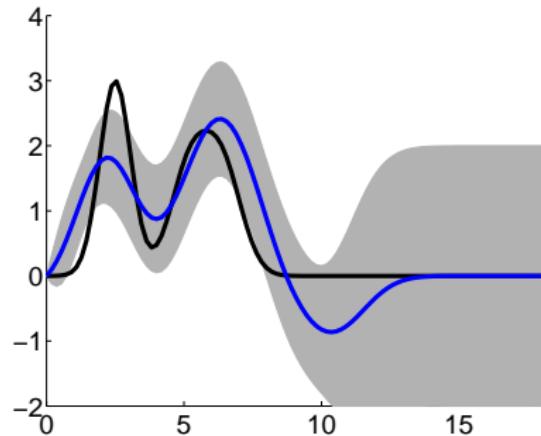
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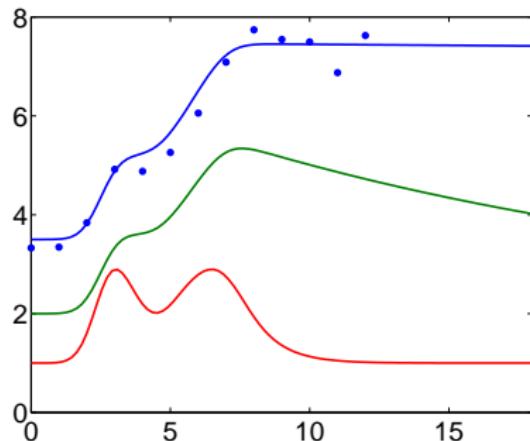
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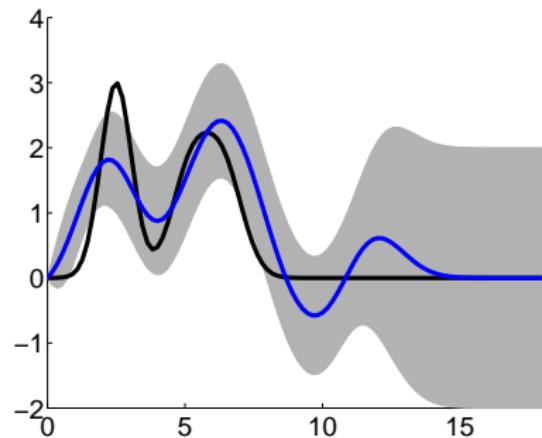
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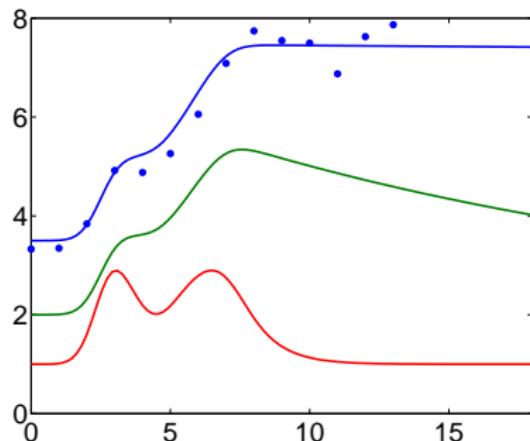
True “gene profiles” and noisy observations.



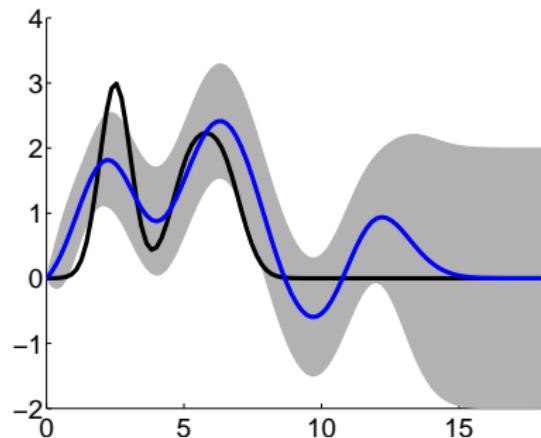
Inferred transcription factor activity.

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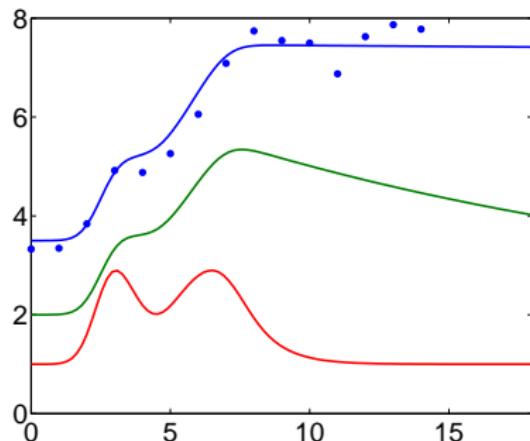
True “gene profiles” and noisy observations.



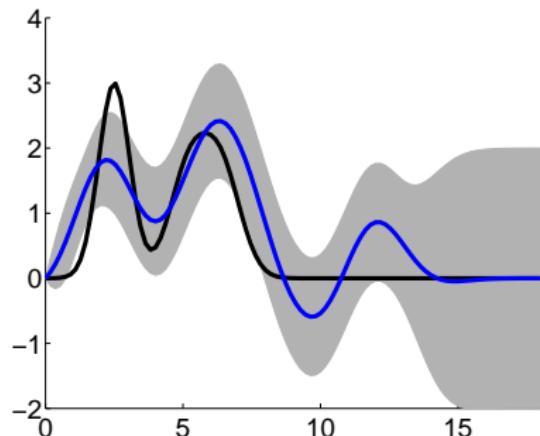
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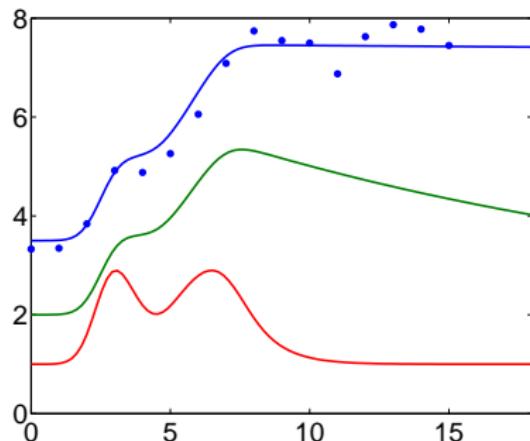
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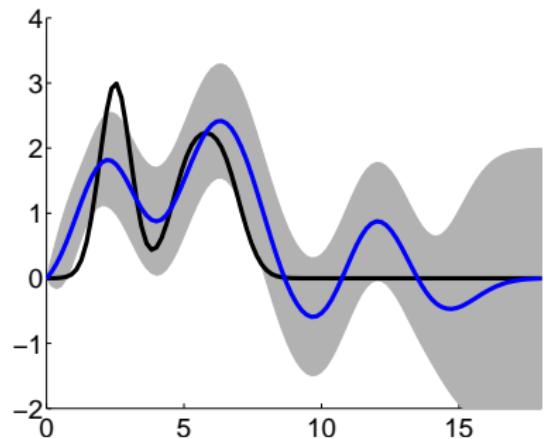
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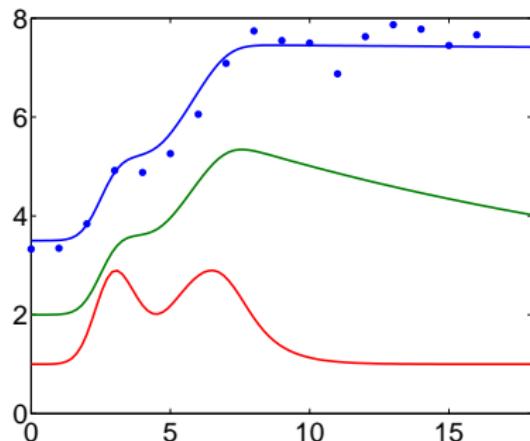
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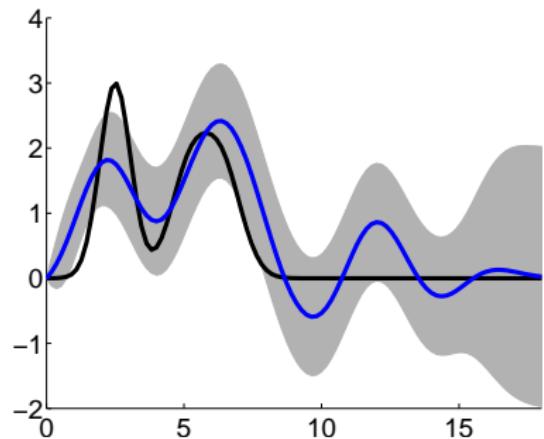
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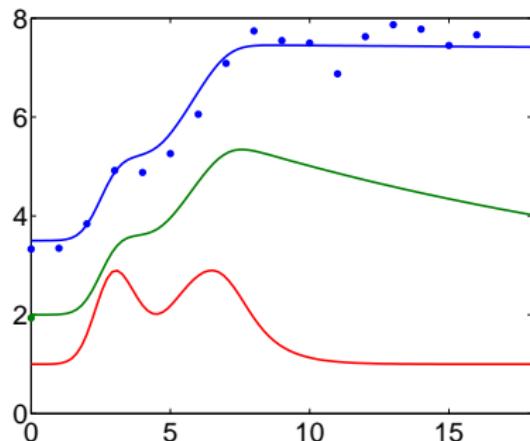
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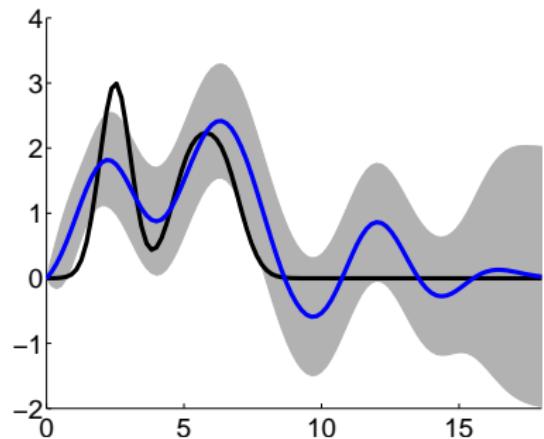
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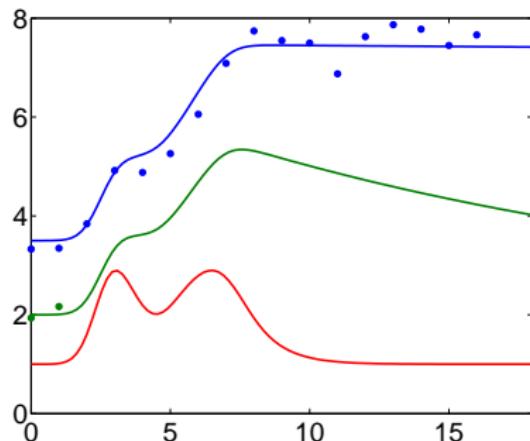
True “gene profiles” and noisy observations.



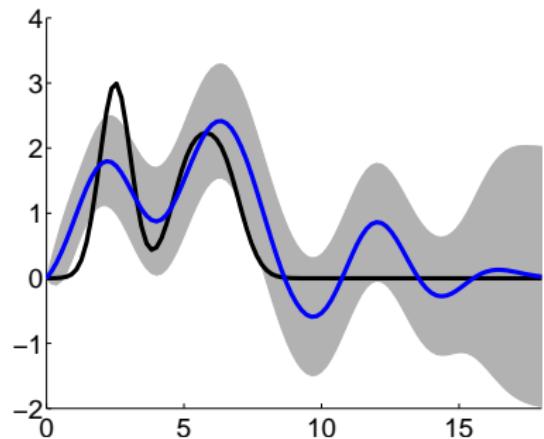
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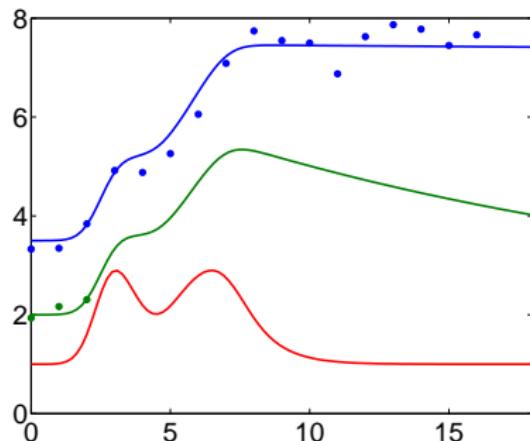
True “gene profiles” and noisy observations.



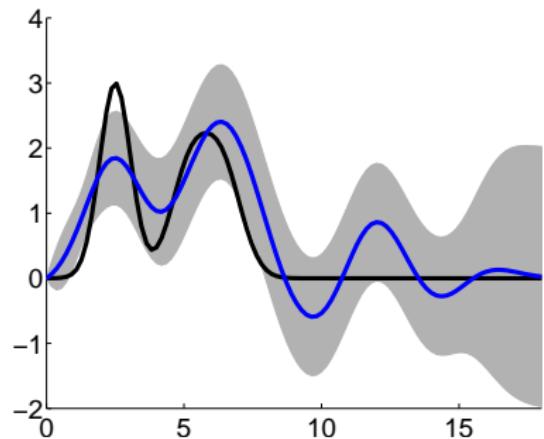
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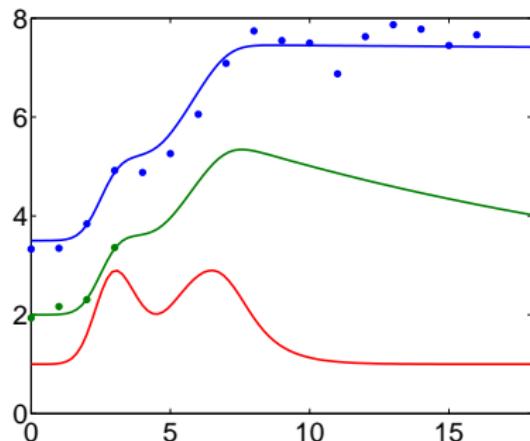
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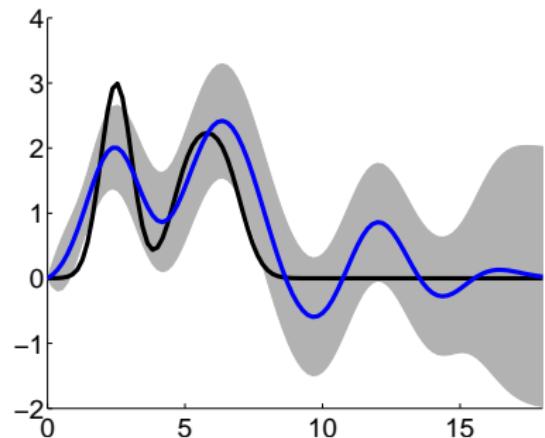
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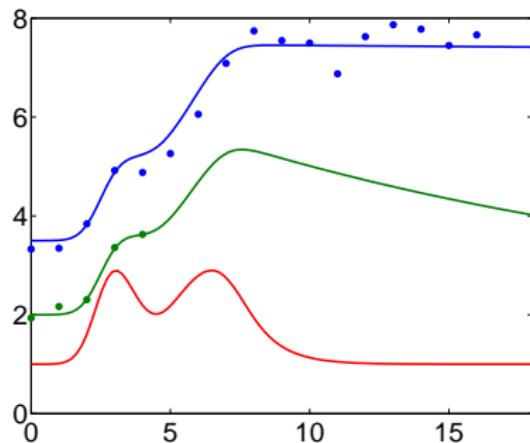
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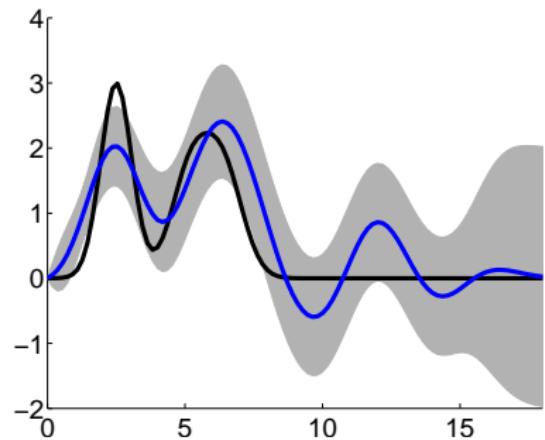
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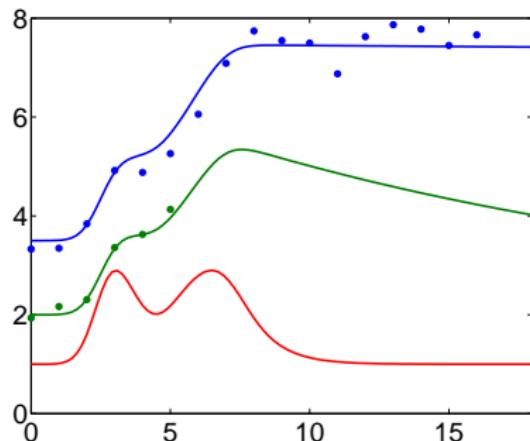
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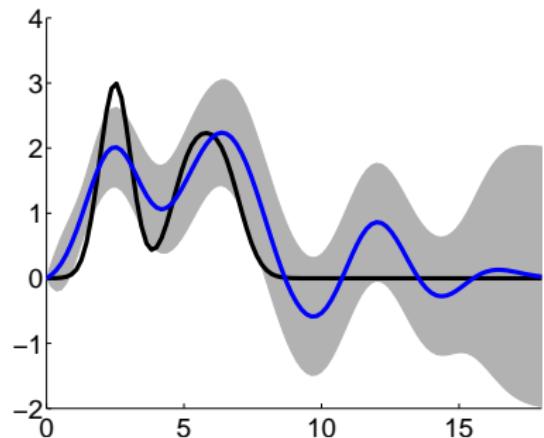
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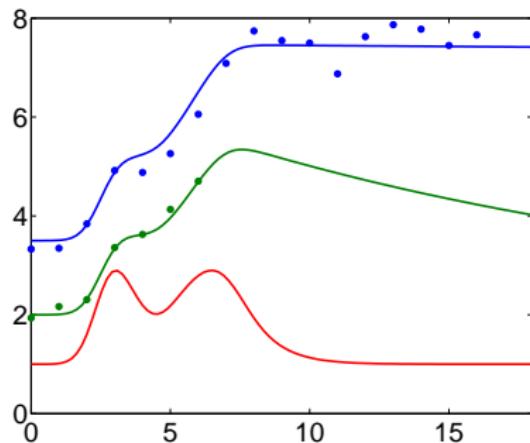
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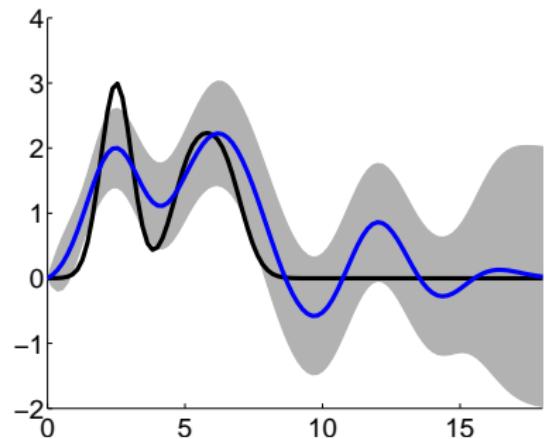
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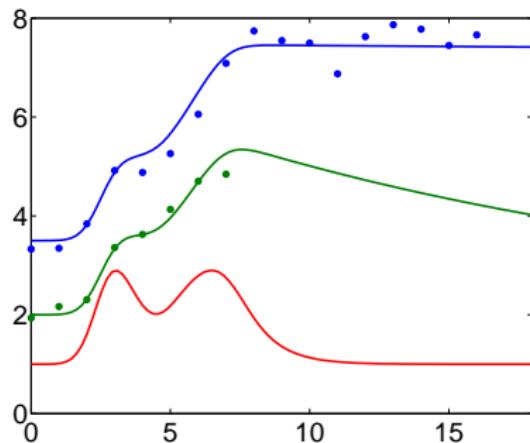
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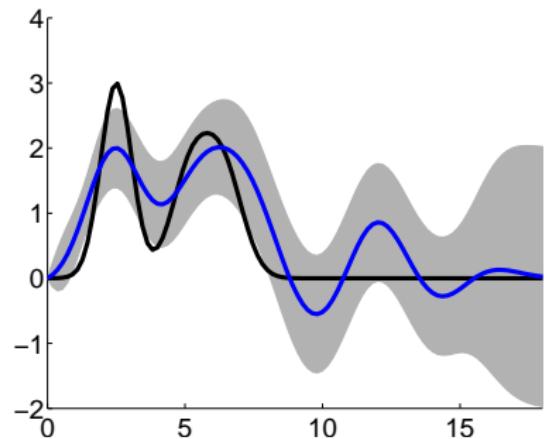
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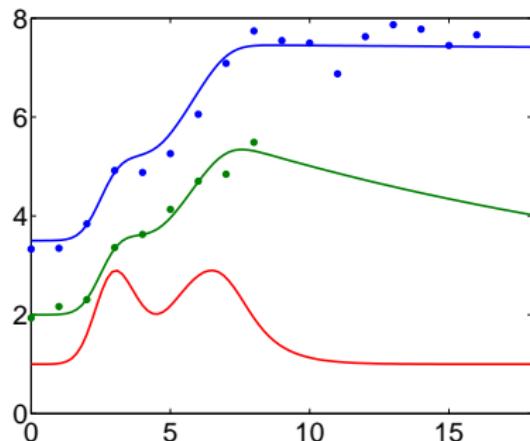
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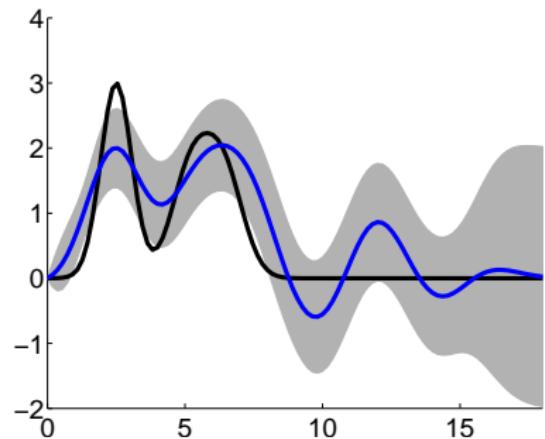
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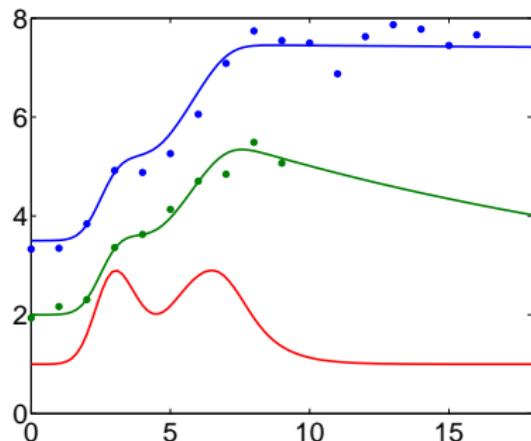
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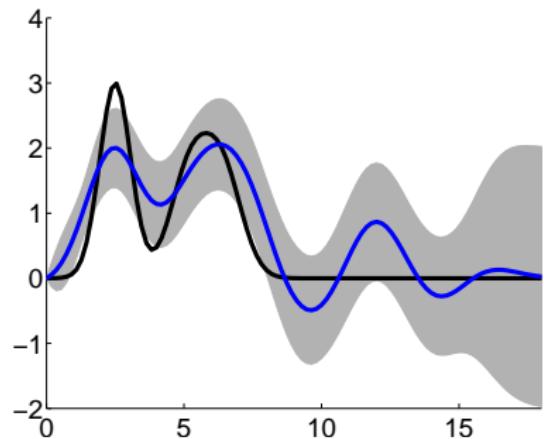
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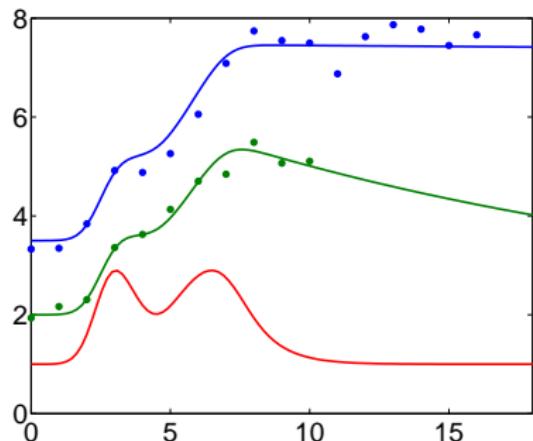
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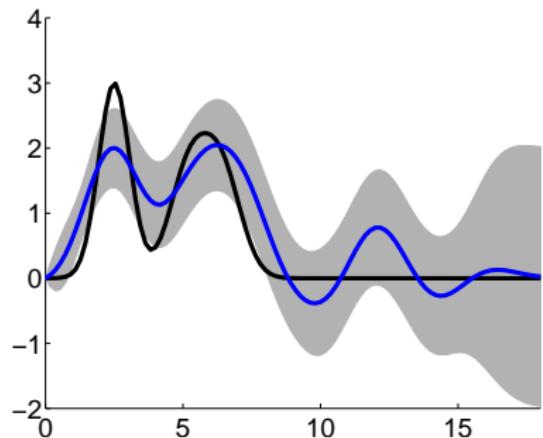
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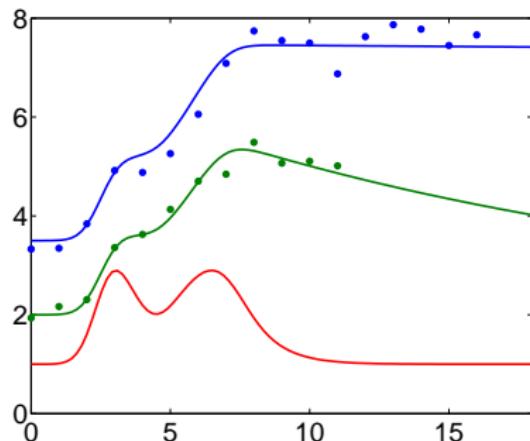
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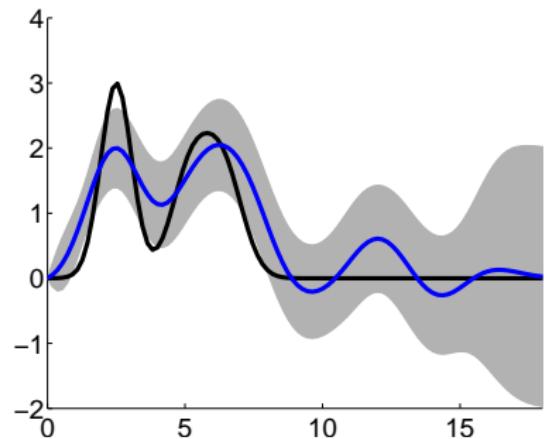
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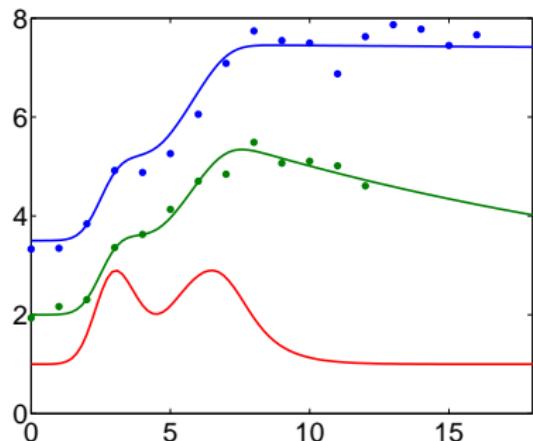
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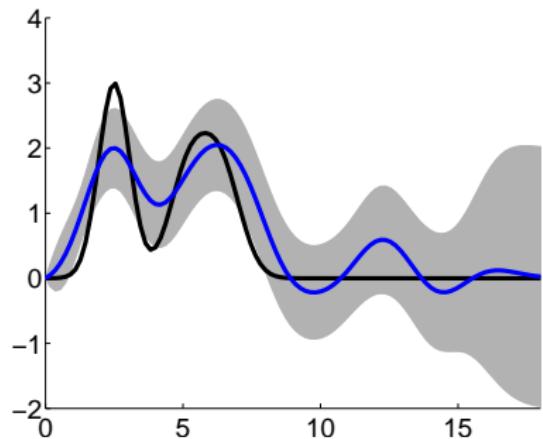
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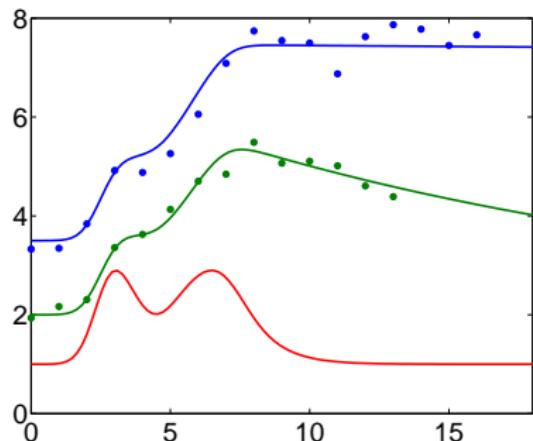
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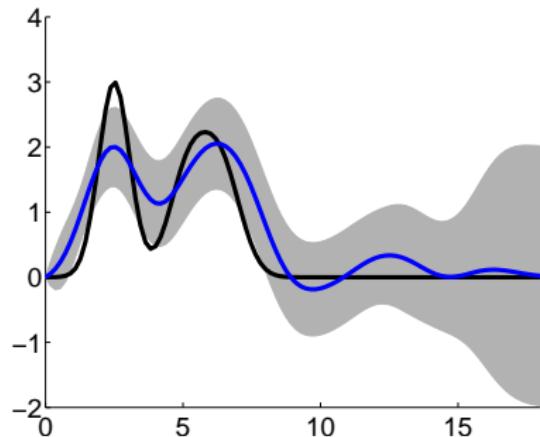
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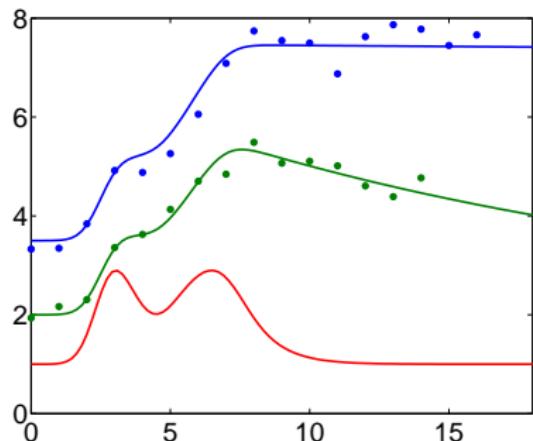
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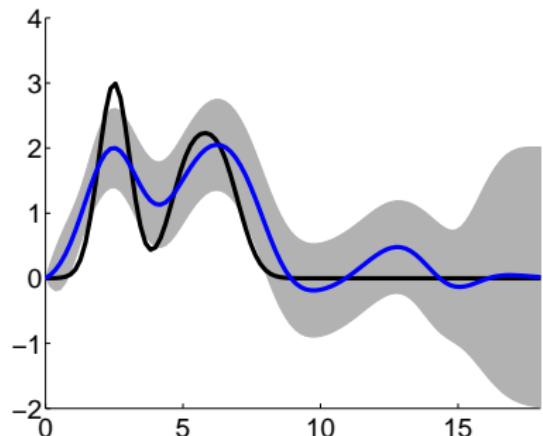
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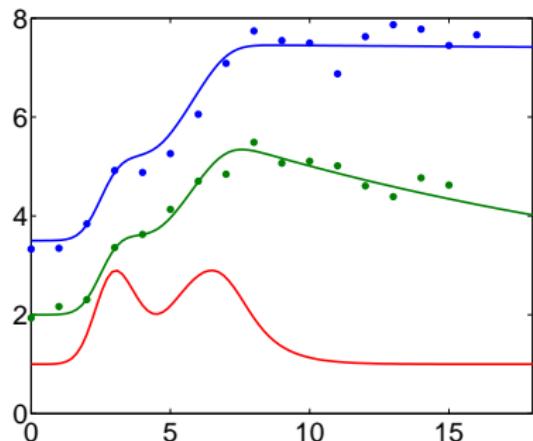
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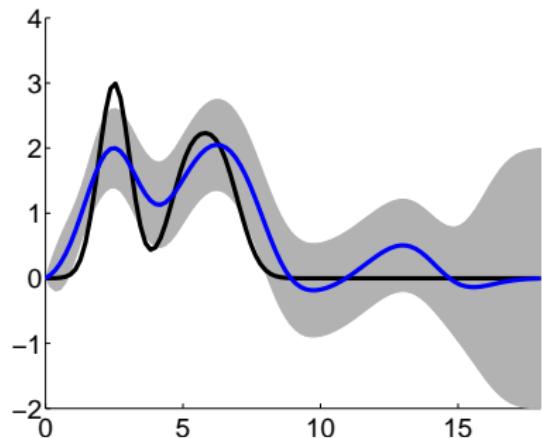
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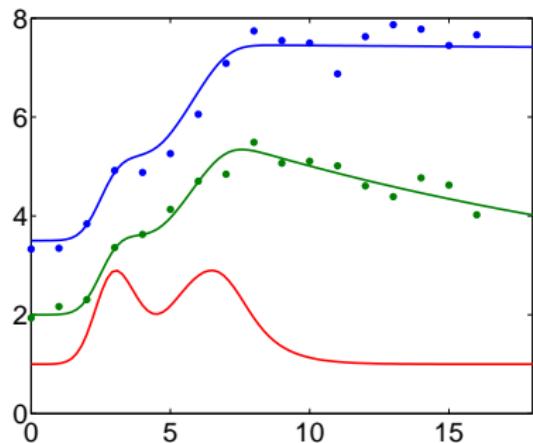
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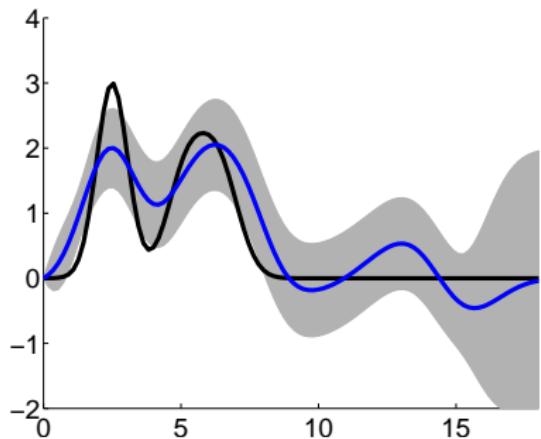
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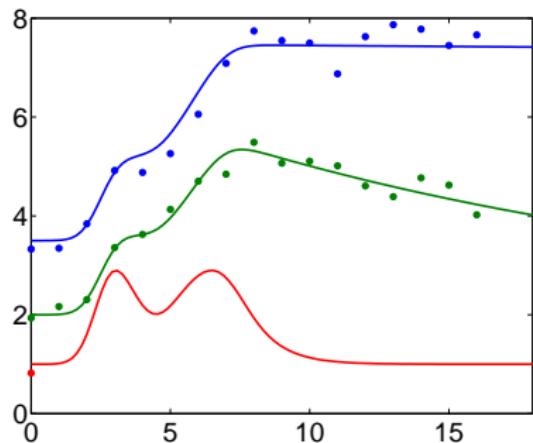
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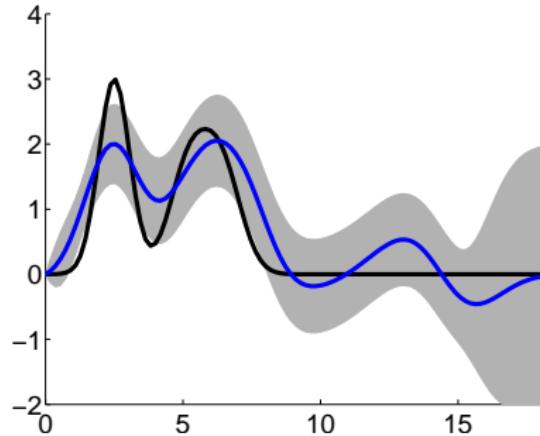
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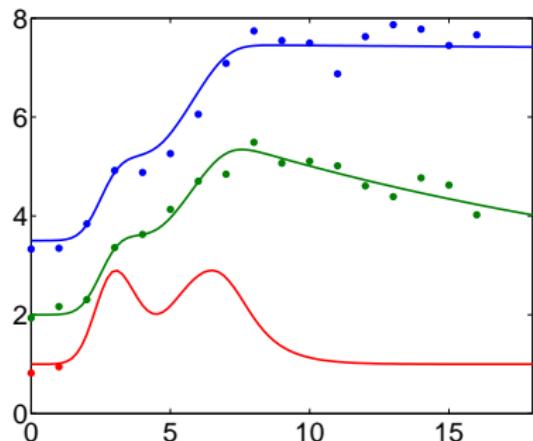
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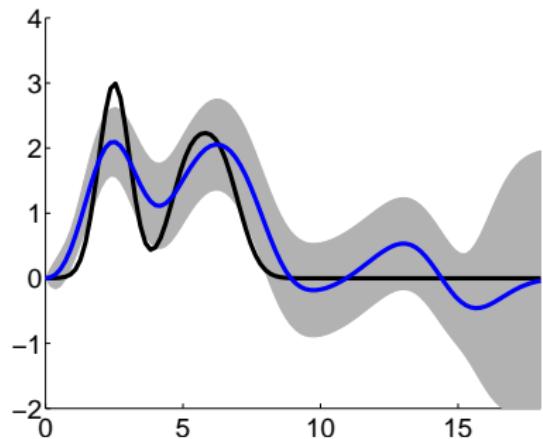
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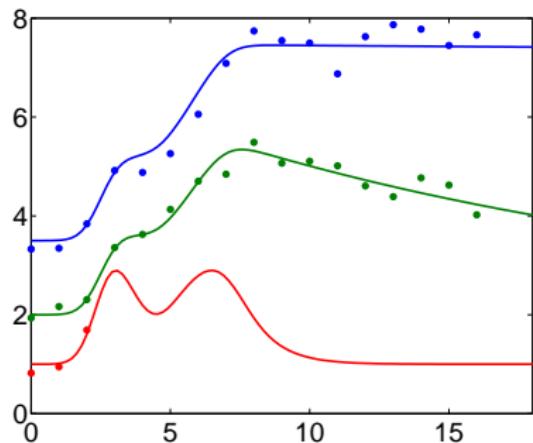
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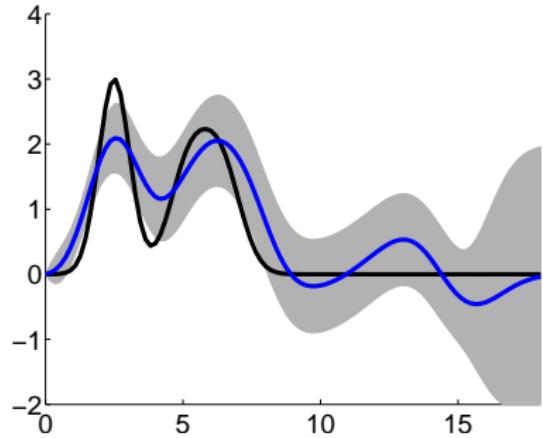
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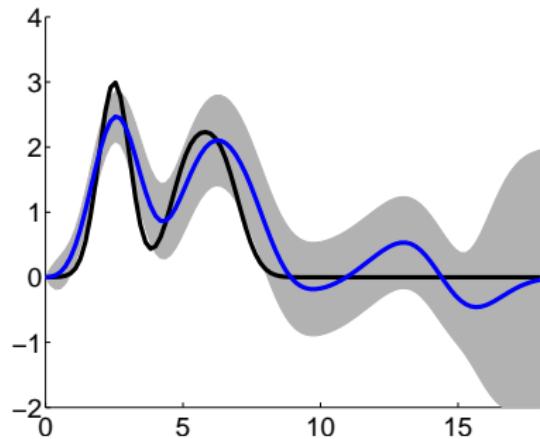
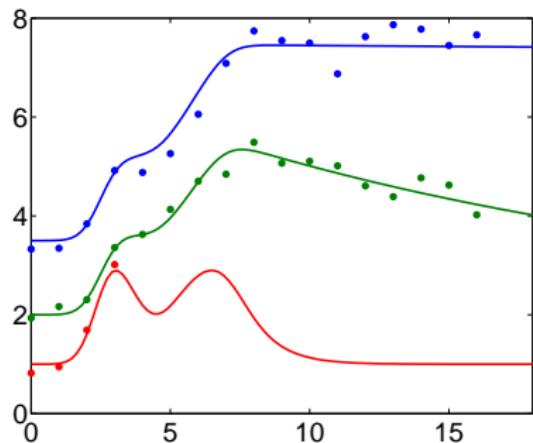
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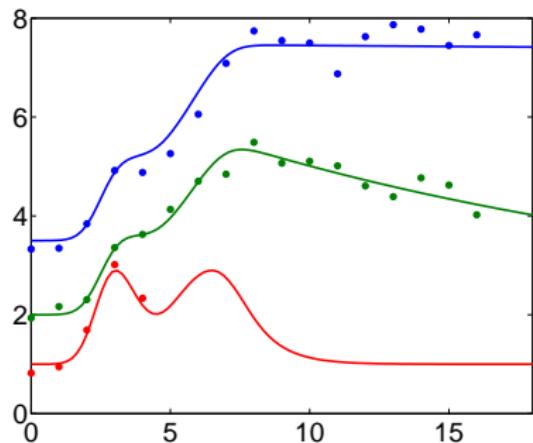
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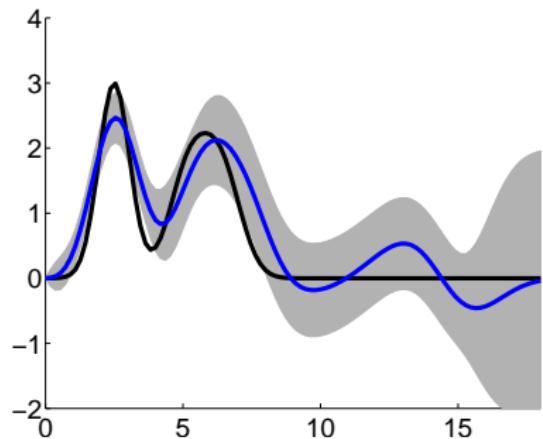


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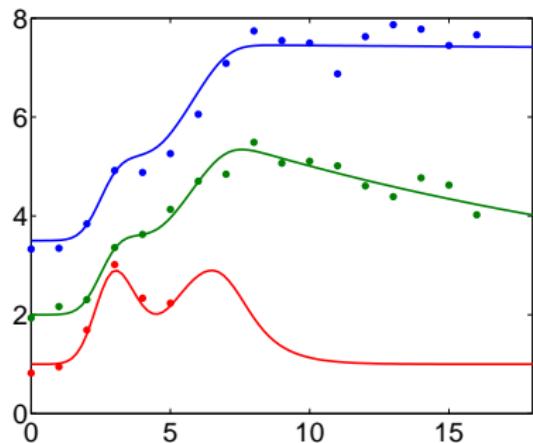
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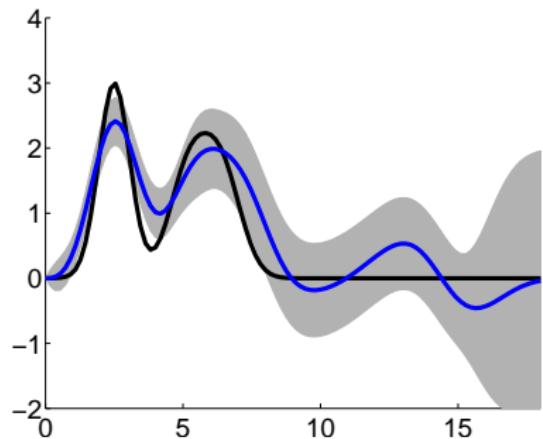
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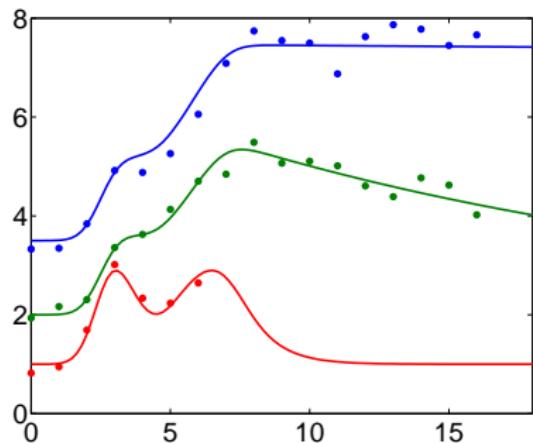
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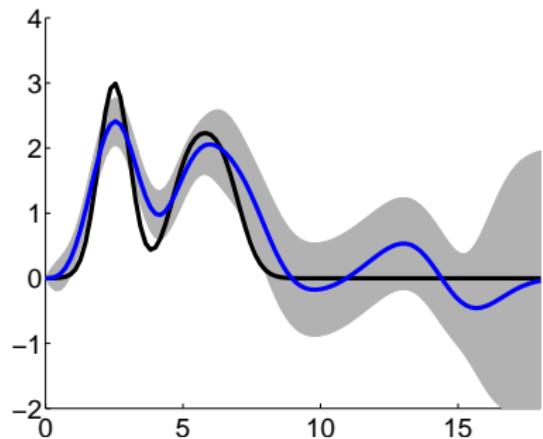
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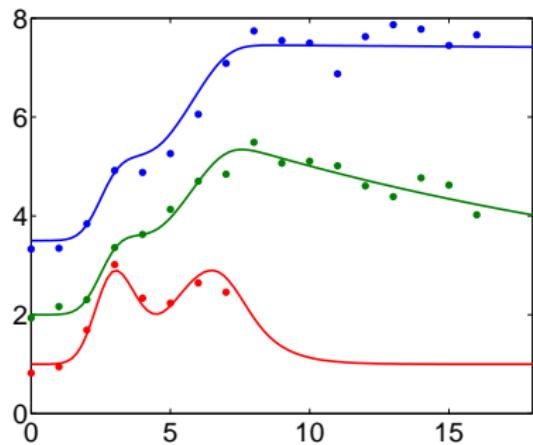
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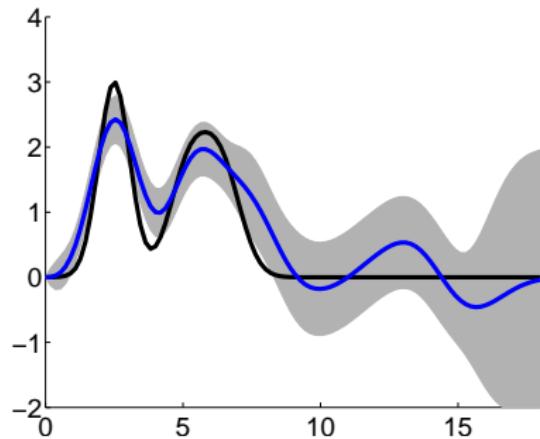
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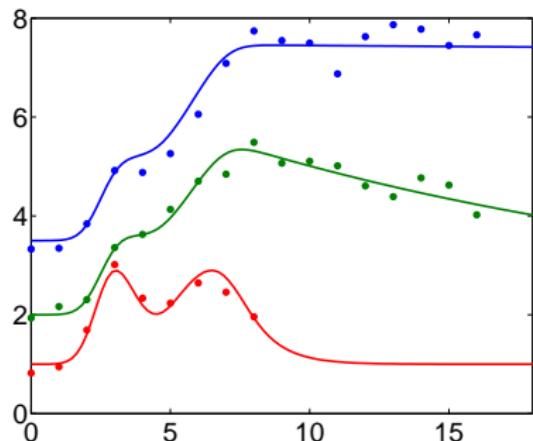
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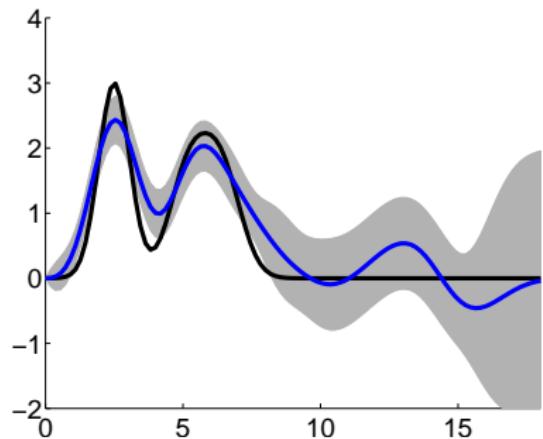
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# Artificial Example: Inferring $p(t)$

Inferring TF activity from artificially sampled genes.



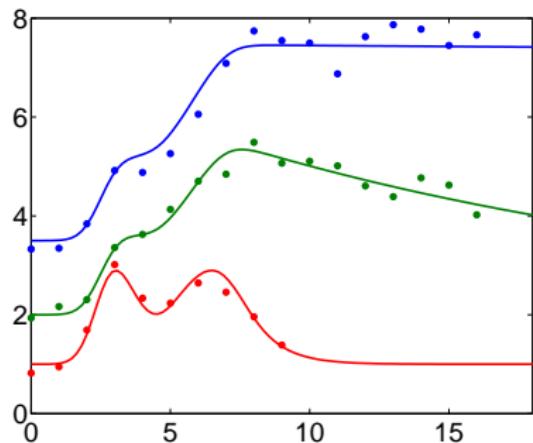
True “gene profiles” and noisy observations.



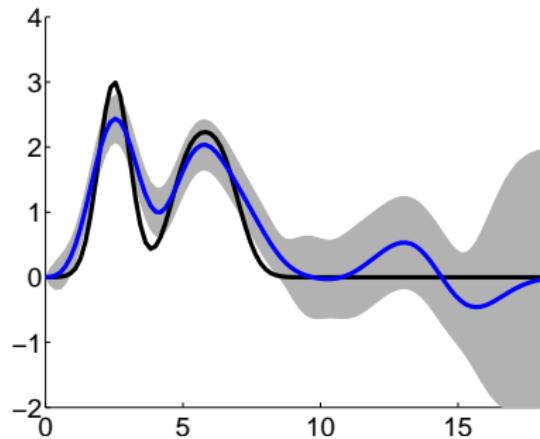
Inferred transcription factor activity.

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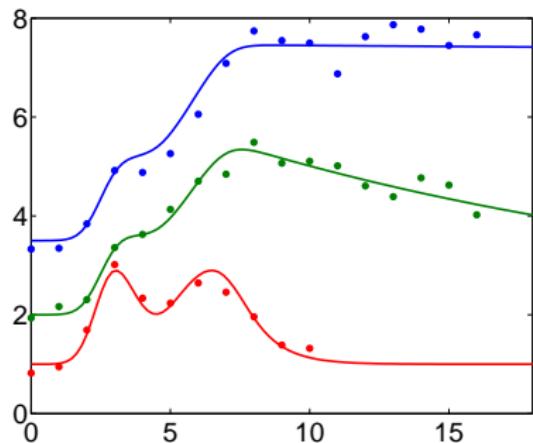
True “gene profiles” and noisy observations.



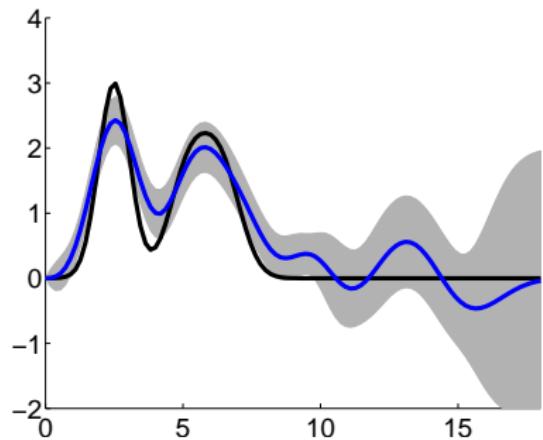
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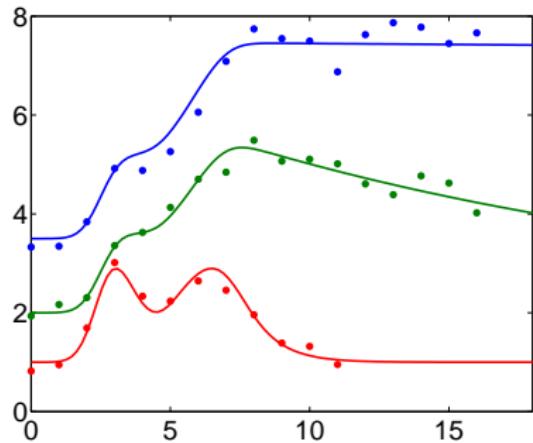
True “gene profiles” and noisy observations.



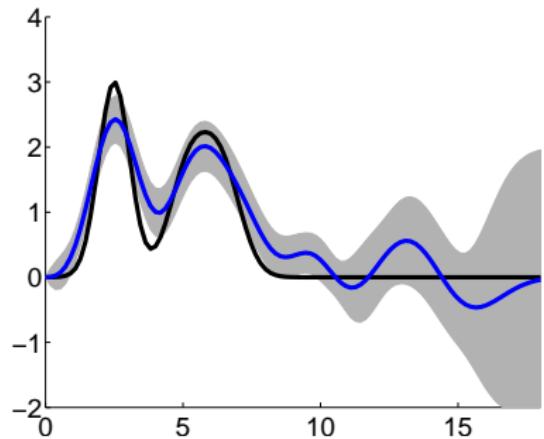
Inferred transcription factor activity.

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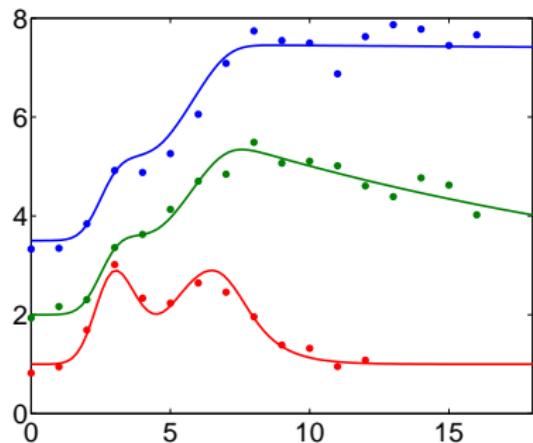
True “gene profiles” and noisy observations.



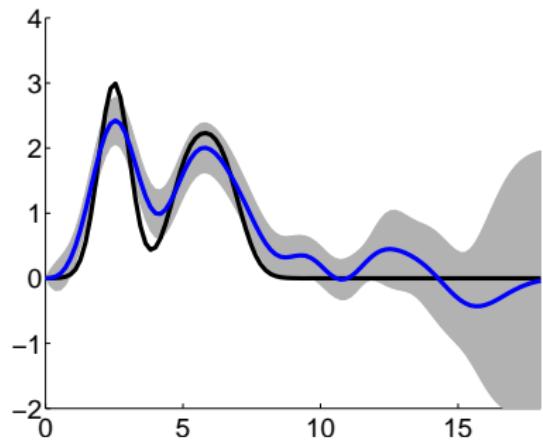
Inferred transcription factor activity.

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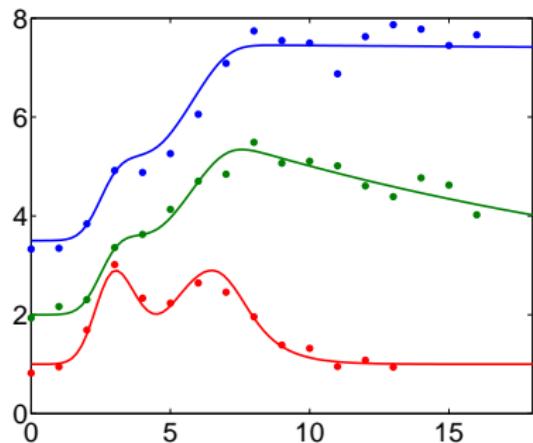
True “gene profiles” and noisy observations.



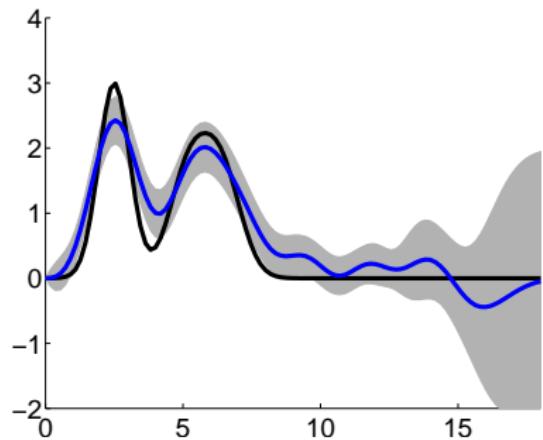
Inferred transcription factor activity.

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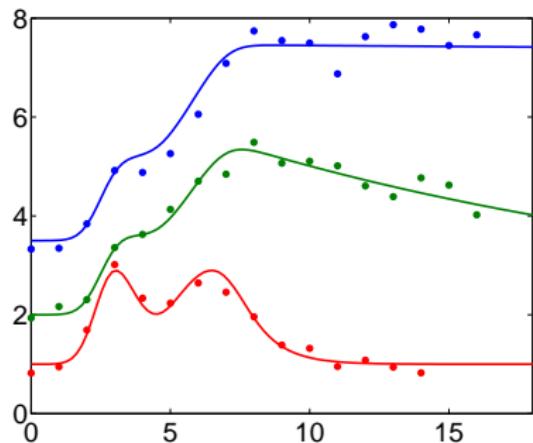
True “gene profiles” and noisy observations.



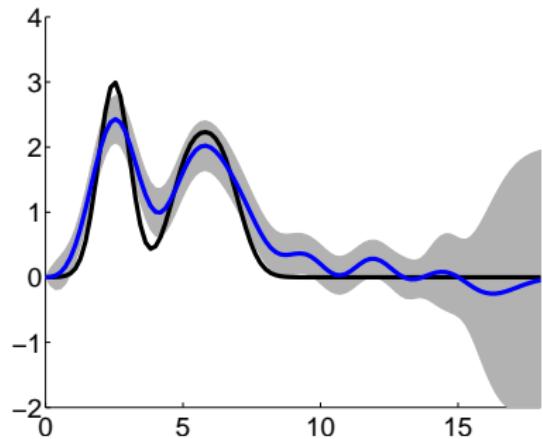
Inferred transcription factor activity.

# Artificial Example: Inferring $p(t)$

Inferring TF activity from artificially sampled genes.



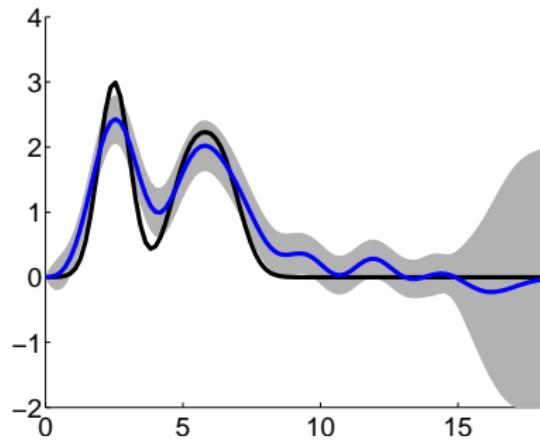
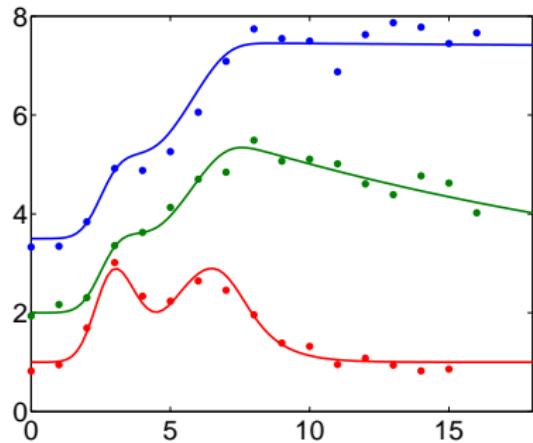
True “gene profiles” and noisy observations.



Inferred transcription factor activity.

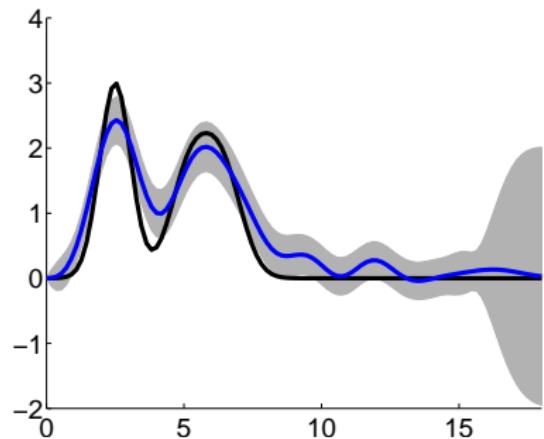
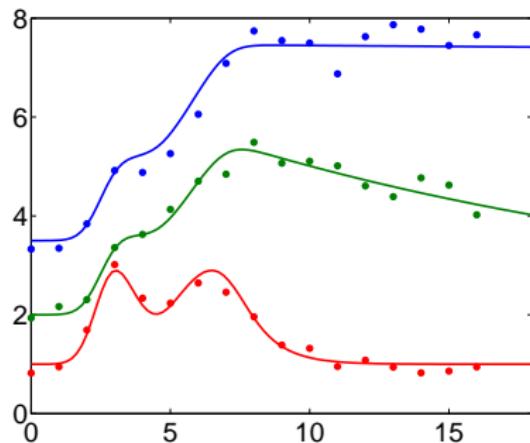
# Artificial Example: Inferring $p(t)$

Inferring TF activity from artificially sampled genes.



# Artificial Example: Inferring $p(t)$

Inferring TF activity from artificially sampled genes.



## Gaussian process modelling of latent chemical species: applications to inferring transcription factor activities

Pei Gao<sup>1</sup>, Antti Honkela<sup>2</sup>, Magnus Rattray<sup>1</sup> and Neil D. Lawrence<sup>1,\*</sup>

<sup>1</sup>School of Computer Science, University of Manchester, Kilburn Building, Oxford Road, Manchester, M13 9PL and

<sup>2</sup>Adaptive Informatics Research Centre, Helsinki University of Technology, PO Box 5400, FI-02015 TKK, Finland

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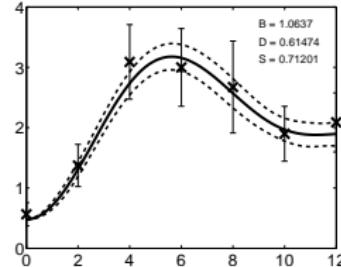
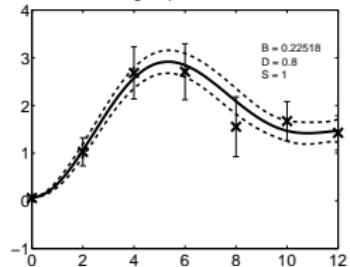
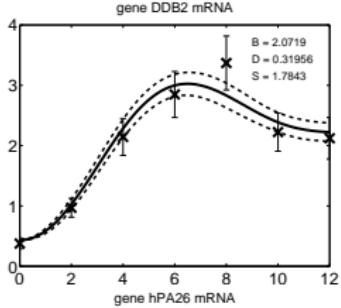
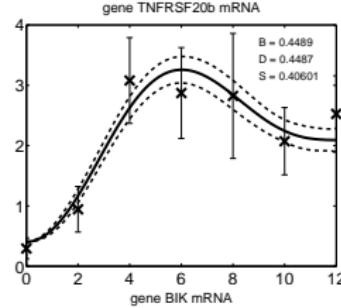
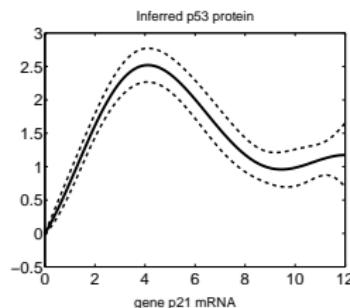
### ABSTRACT

**Motivation:** Inference of *latent chemical species* in biochemical interaction networks is a key problem in estimation of the structure

A challenging problem for parameter estimation in ODE models occurs where one or more chemical species influencing the dynamics are controlled outside of the sub-system being modelled. For

# p53 Results with GP

(Gao et al., 2008)

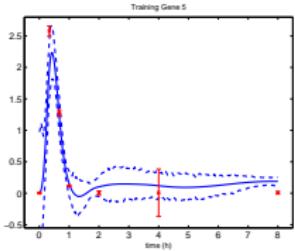
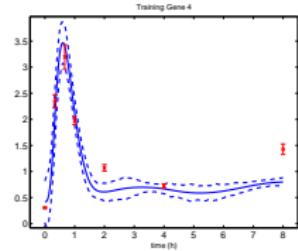
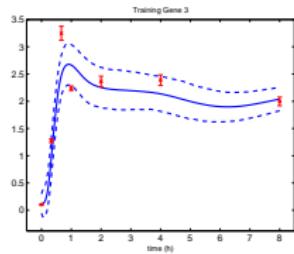
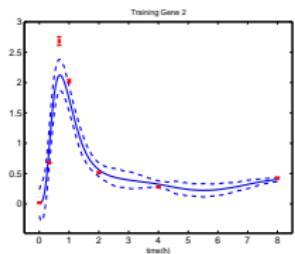
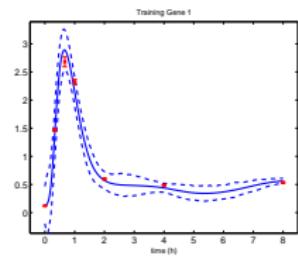
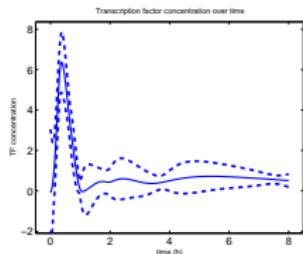


## Ranking with ERK Signalling

- ▶ Target Ranking for Elk-1.
- ▶ Elk-1 is phosphorylated by ERK from the EGF signalling pathway.
- ▶ Predict concentration of Elk-1 from known targets.
- ▶ Rank other targets of Elk-1.

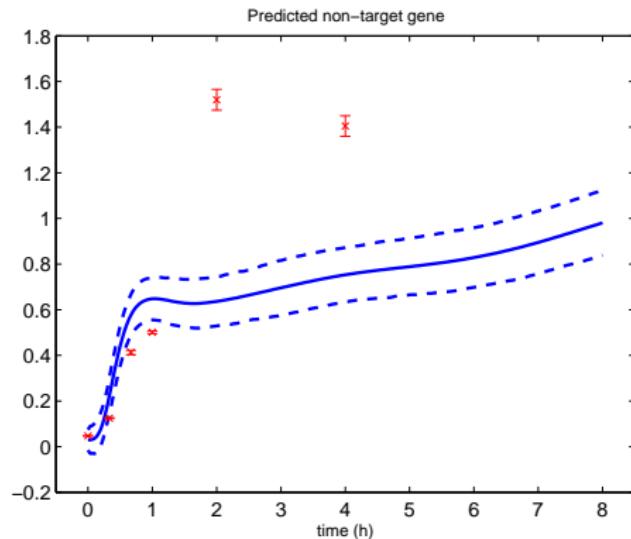
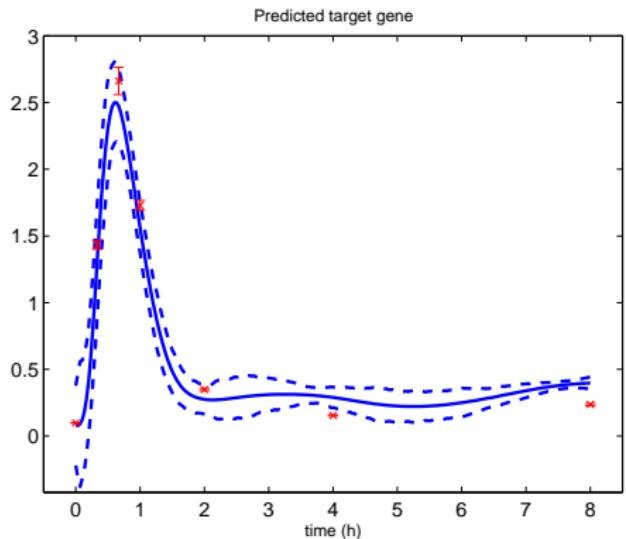
# Elk-1 (MLP covariance)

Jennifer Withers



# Elk-1 target selection

Fitted model used to rank potential targets of Elk-1



# Outline

Motivation

Cascade Differential Equations

Discussion and Future Work

## Model-based method for transcription factor target identification with limited data

Antti Honkela<sup>a,1</sup>, Charles Girardot<sup>b</sup>, E. Hilary Gustafson<sup>b</sup>, Ya-Hsin Liu<sup>b</sup>, Eileen E. M. Furlong<sup>b</sup>, Neil D. Lawrence<sup>c,1</sup>, and Magnus Rattray<sup>c,1</sup>

<sup>a</sup>Department of Information and Computer Science, Aalto University School of Science and Technology, Helsinki, Finland; <sup>b</sup>Genome Biology Unit, European Molecular Biology Laboratory, Heidelberg, Germany; and <sup>c</sup>School of Computer Science, University of Manchester, Manchester, United Kingdom

Edited by David Baker, University of Washington, Seattle, WA, and approved March 3, 2010 (received for review December 10, 2009)

**We present a computational method for identifying potential targets of a transcription factor (TF) using wild-type gene expression time series data. For each putative target gene we fit a simple differential equation model of transcriptional regulation, and the**

used for genome-wide scoring of putative target genes. A key consideration is required to apply our method is wild-type time series data that are collected over a period where TF activity is changing. Our method allows for complementary evidence from expression

# Cascaded Differential Equations

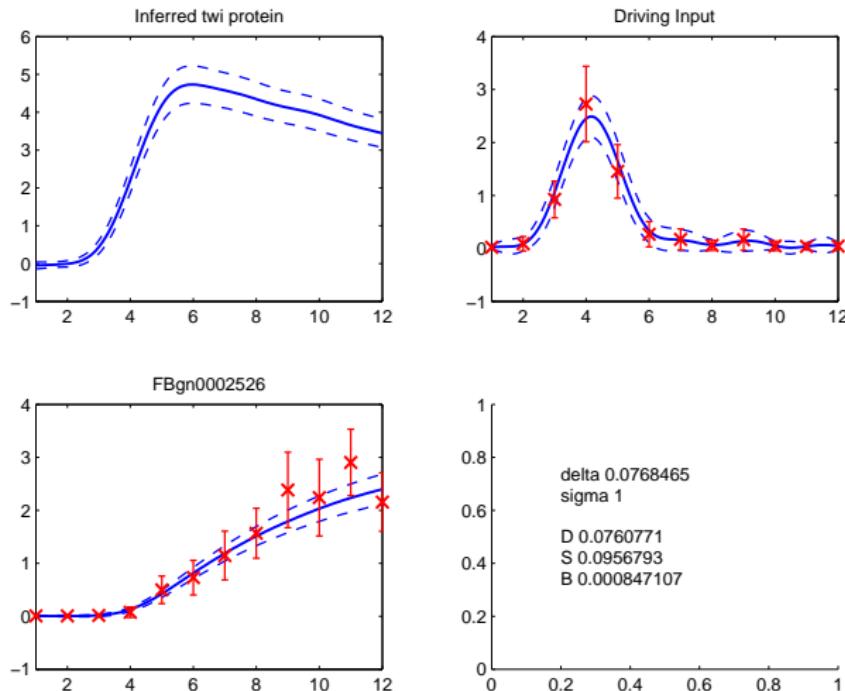
(Honkela et al., 2010)

- ▶ Transcription factor protein also has governing mRNA.
- ▶ This mRNA can be measured.
- ▶ In signalling systems this measurement can be misleading because it is activated (phosphorylated) transcription factor that counts.
- ▶ In development phosphorylation plays less of a role.

## Twist Results

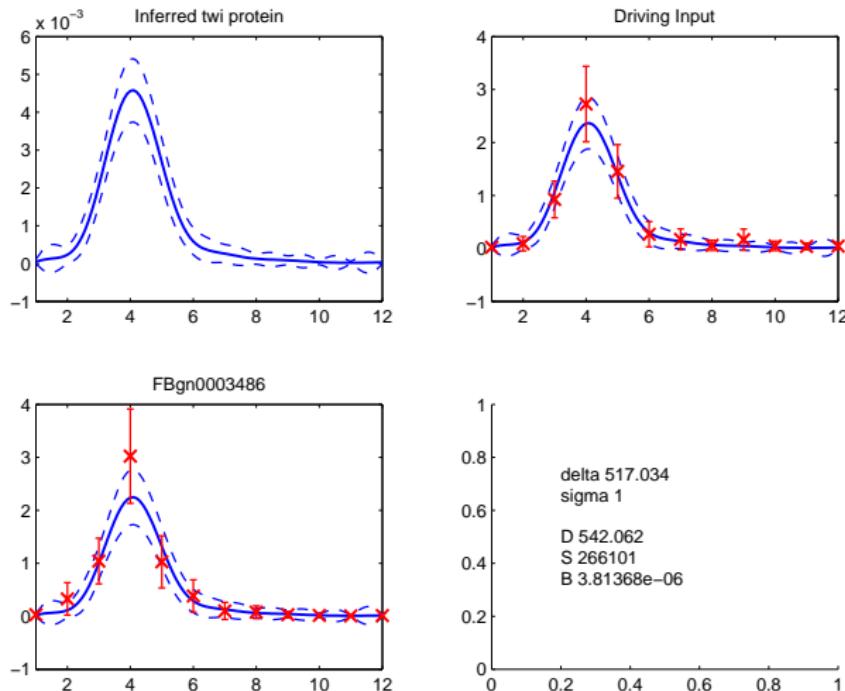
- ▶ Use mRNA of Twist as driving input.
- ▶ For each gene build a cascade model that forces Twist to be the only TF.
- ▶ Compare fit of this model to a baseline (e.g. similar model but sensitivity zero).
- ▶ Rank according to the likelihood above the baseline.
- ▶ Compare with correlation, knockouts and time series network identification (TSNI) (Della Gatta et al., 2008).

# Results for Twi using the Cascade model



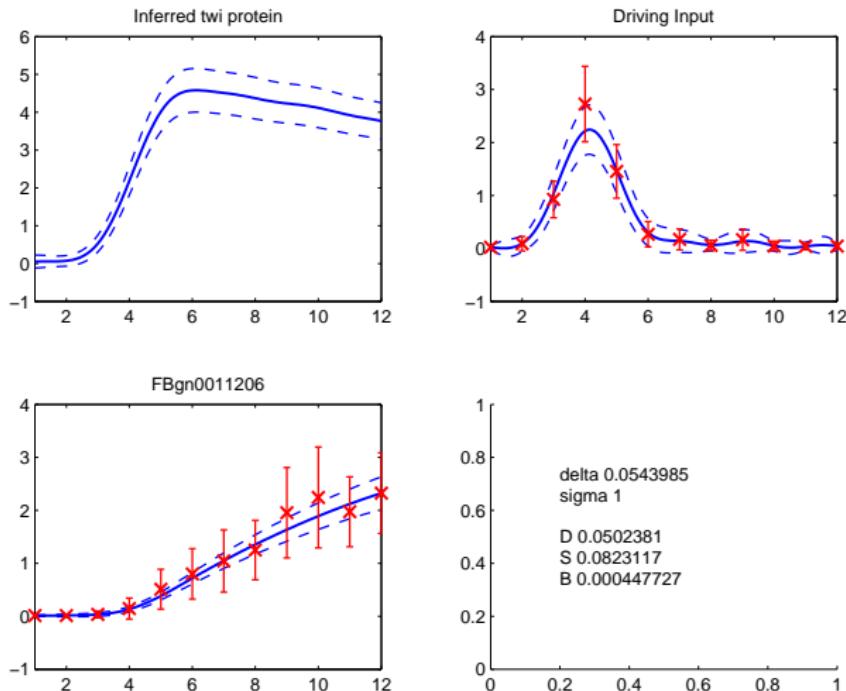
**Figure:** Model for flybase gene identity FBgn0002526.

# Results for Twi using the Cascade model



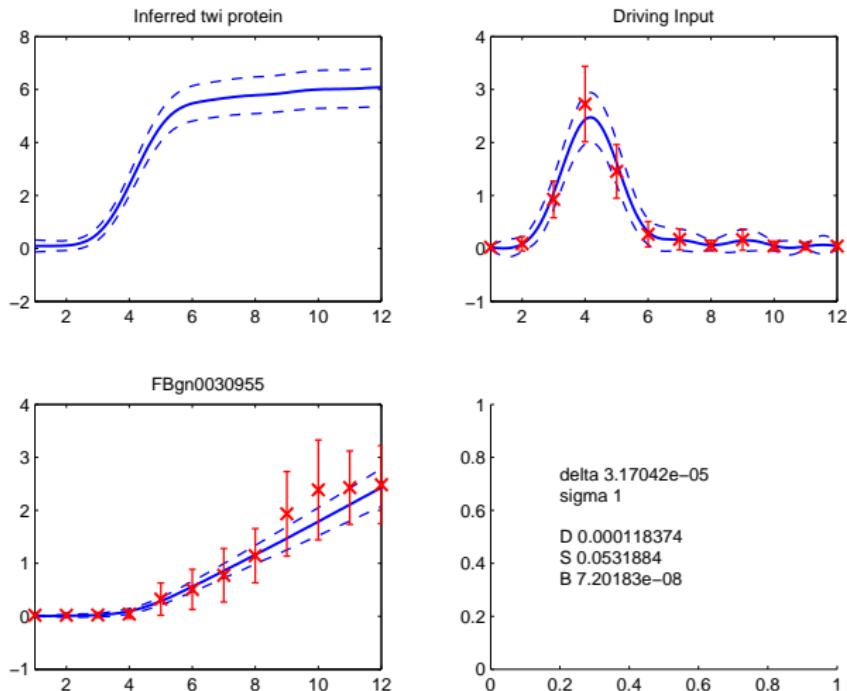
**Figure:** Model for flybase gene identity FBgn0003486.

# Results for Twi using the Cascade model



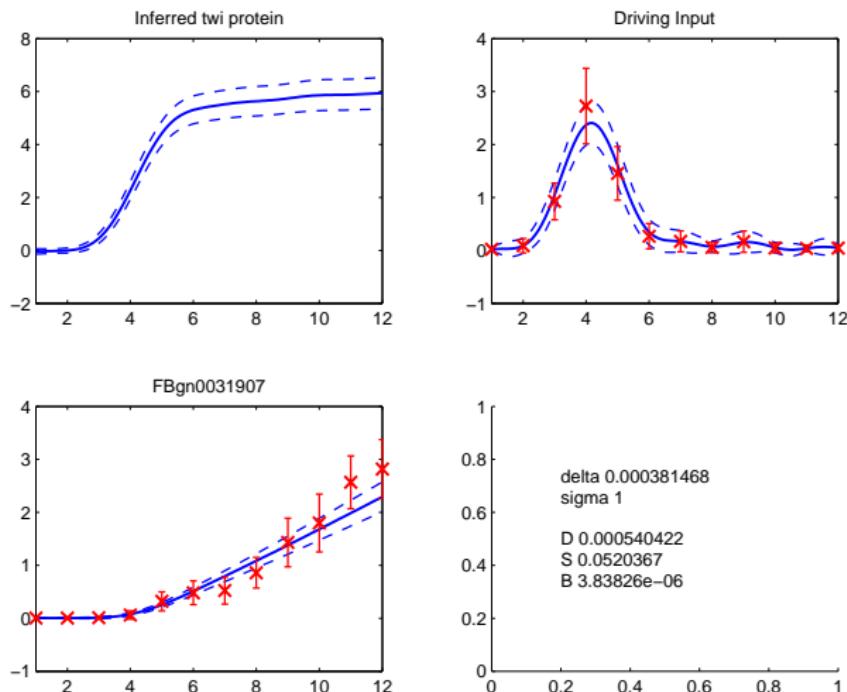
**Figure:** Model for flybase gene identity FBgn0011206.

# Results for Twi using the Cascade model



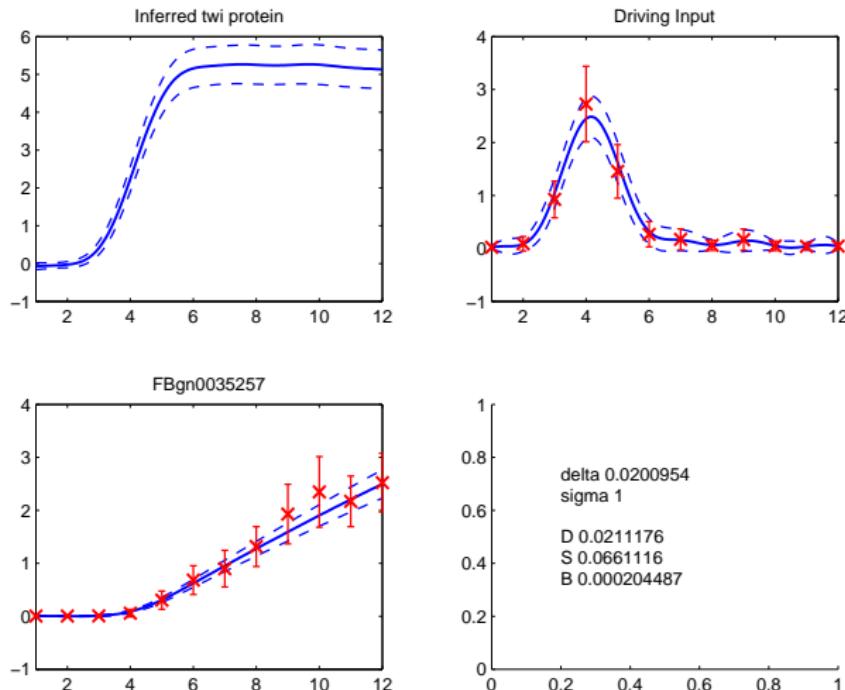
**Figure:** Model for flybase gene identity FBgn00309055.

# Results for Twi using the Cascade model



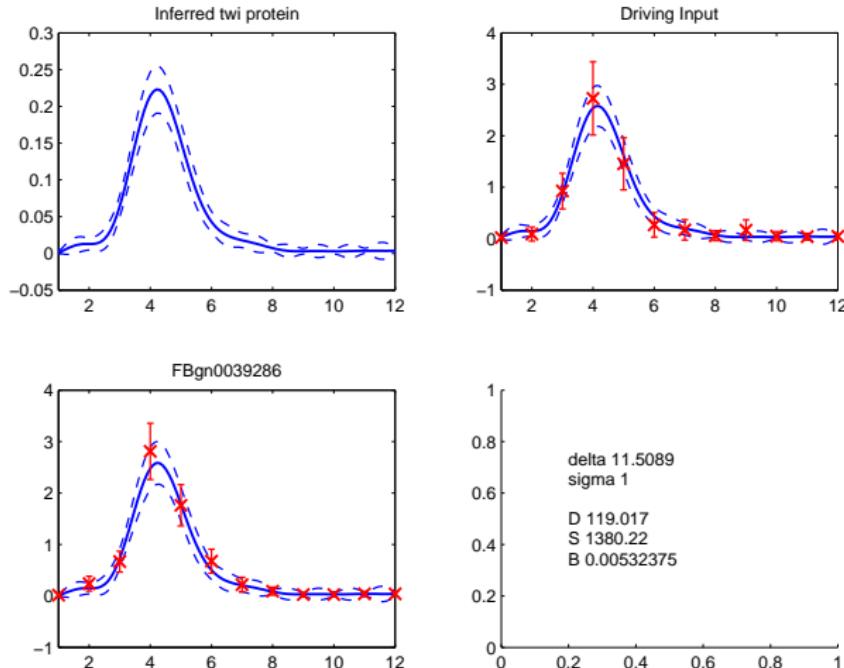
**Figure:** Model for flybase gene identity FBgn0031907.

# Results for Twi using the Cascade model



**Figure:** Model for flybase gene identity FBgn0035257.

# Results for Twi using the Cascade model

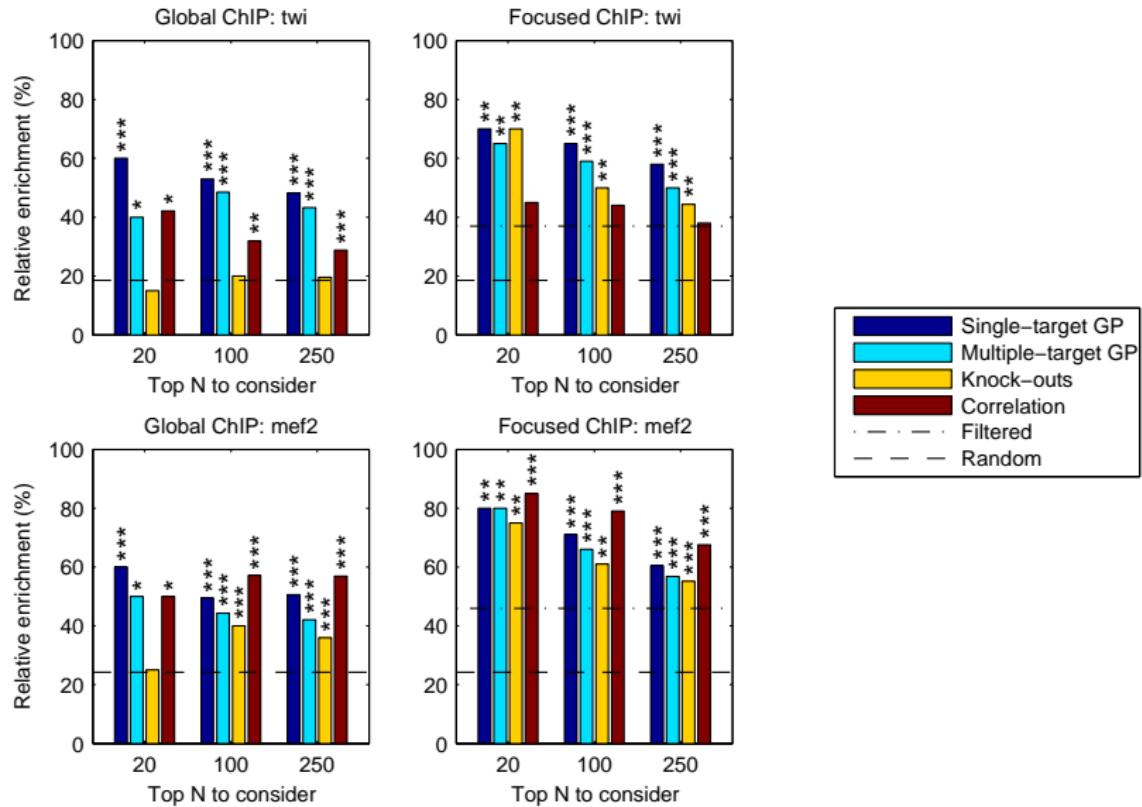


**Figure:** Model for flybase gene identity FBgn0039286.

## Evaluation methods

- ▶ Evaluate the ranking methods by taking a number of top-ranked targets and record the number of "positives" (Zinzen et al., 2009):
  - ▶ targets with ChIP-chip binding sites within 2 kb of gene
  - ▶ (targets differentially expressed in TF knock-outs)
- ▶ Compare against
  - ▶ Ranking by correlation of expression profiles
  - ▶ Ranking by  $q$ -value of differential expression in knock-outs
- ▶ Optionally focus on genes with annotated expression in tissues of interest

# Results



\*\*\*\*:  $p < 0.001$ , \*\*:  $p < 0.01$ , \*:  $p < 0.05$

## Summary

- ▶ Cascade models allow genomewide analysis of potential targets given only expression data.
- ▶ Once a set of potential candidate targets have been identified, they can be modelled in a more complex manner.
- ▶ We don't have ground truth, but evidence indicates that the approach *can* perform as well as knockouts.

# Outline

Motivation

Cascade Differential Equations

Discussion and Future Work

## Discussion and Future Work

- ▶ Integration of probabilistic inference with mechanistic models.
- ▶ Software available through bioconductor (TIGRE Package)  
<http://bioconductor.org/packages/2.6/bioc/html/tigre.html>.
- ▶ Applications in modeling gene expression.
- ▶ Ongoing/other work:
  - ▶ Non linear response and non linear differential equations.
  - ▶ Improving computational complexity.
  - ▶ Stochastic differential equations.
  - ▶ Cascade model introduces model of translation.

## Acknowledgements

- ▶ Investigators: Neil Lawrence and Magnus Rattray
- ▶ Researchers: Pei Gao, Antti Honkela, Guido Sanguinetti, Michalis Titsias.
- ▶ Martino Barenco and Mike Hubank at the Institute of Child Health in UCL (p53 pathway).
- ▶ Charles Girardot and Eileen Furlong of EMBL in Heidelberg (mesoderm development in *D. Melanogaster*).

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# References I

- M. Barenco, D. Tomescu, D. Brewer, R. Callard, J. Stark, and M. Hubank. Ranked prediction of p53 targets using hidden variable dynamic modeling. *Genome Biology*, 7(3):R25, 2006.
- G. Della Gatta, M. Bansal, A. Ambesi-Impiombato, D. Antonini, C. Missero, and D. di Bernardo. Direct targets of the trp63 transcription factor revealed by a combination of gene expression profiling and reverse engineering. *Genome Research*, 18(6):939–948, Jun 2008. [\[URL\]](#). [\[DOI\]](#).
- P. Gao, A. Honkela, M. Rattray, and N. D. Lawrence. Gaussian process modelling of latent chemical species: Applications to inferring transcription factor activities. *Bioinformatics*, 24:i70–i75, 2008. [\[PDF\]](#). [\[DOI\]](#).
- D. S. Goodsell. The molecular perspective: p53 tumor suppressor. *The Oncologist*, Vol. 4, No. 2, 138-139, April 1999, 4(2):138–139, 1999.
- A. Honkela, C. Girardot, E. H. Gustafson, Y.-H. Liu, E. E. M. Furlong, N. D. Lawrence, and M. Rattray. Model-based method for transcription factor target identification with limited data. *Proc. Natl. Acad. Sci. USA*, 107(17):7793–7798, Apr 2010. [\[DOI\]](#).
- Y. Lazebnik. Can a biologist fix a radio? or, what I learned while studying apoptosis. *Cancer Cell*, 2:179–182, 2002.
- S. T. Roweis. EM algorithms for PCA and SPCA. In M. I. Jordan, M. J. Kearns, and S. A. Solla, editors, *Advances in Neural Information Processing Systems*, volume 10, pages 626–632, Cambridge, MA, 1998. MIT Press.
- M. E. Tipping and C. M. Bishop. Probabilistic principal component analysis. *Journal of the Royal Statistical Society, B*, 6(3):611–622, 1999. [\[PDF\]](#). [\[DOI\]](#).
- R. P. Zinzen, C. Girardot, J. Gagneur, M. Braun, and E. E. M. Furlong. Combinatorial binding predicts spatio-temporal cis-regulatory activity. *Nature*, 462(7269):65–70, Nov 2009. [\[URL\]](#). [\[DOI\]](#).